Testing Growth Theory Using Existing Growth Models for MENA Countries

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Abstract
This paper examines the growing gap between the theoretical and empirical growth literature and policy needs of the developing economies. Growth literature has focused mainly on long term growth outcomes, but policy makers of the developing economies need rapid improvements in the short to medium term growth rates. In this paper we argue that this gap can be reduced by distinguishing between the short to medium term dynamic effects of policies from their long run equilibrium effects. With data from selected 15 MENA countries; we show that an extended version of the Solow (1956) model is well suited for this purpose. We include the education finding that the short to medium term growth effects of the investment ratio are quite significant and they may persist for up to 10 years.

Keywords: Solow growth model, endogenous growth, dynamic growth effects of investment ratio, policies for developing countries

1. Introduction

Only a few empirical studies have dealt with the MENA region largely due to lack of data. However, as data became available for some countries of the region, some researchers have addressed these countries in the context of a large sample. Among the early studies to estimate the physical stocks and analysis the source of growth is that Nehru and Dhareshwar (1993), Aamer, Abu-Quarn, and Abu-Bader (2007). They used different methods to estimate physical capital and to estimate the production function.

One the most notable and broadly-shared characteristics of MENA economics is the fast growth of population and the increase of labour force. From 1980s until 1990s the economic growth in MENA still unchanged because of the collapse in investment and instability of macroeconomic variables in the region (Keller & Nabli, 2002). In addition, in 2000s there is increase of public investment in infrastructure, health and education was able to translate into high growth of GDP.

In terms of labour market, the World Bank (2004) has documented that MENA’s total labour force has been experiencing an unprecedented expansion—from 104 million workers in 2000 to an estimated by 146 million by 2010 and to an expected 185 million by 2020. So, it is so hard for these countries to create the millions of job needed to absorb this rapid expansion of work force, resulting in the region experiencing the highest level of unemployment in the world. Additionally, the growth contribution of labour seems to have been rising over time because of a general acceleration in labour supply growth in the region over the last period (Esfahani, 2008).

Another salient feature of the recent growth of real GDP performance of MENA countries is its high volatility. It is shown in the Appendix B that during the period 1970-1980, the average of real GDP growth of MENA countries has been characterized by a high variability. On the other hand, the average of real GDP in MENA oil-exporters countries is much more volatile than the non-oil countries.

2. Model Specification and Data Description

The analytical framework of this study is discussed in four sub-sections. We specify the production function for long-run and short-run for fifteen MENA countries in the first section, followed by the definition of the variables in the model and the sources of our data. The third section presents the review of estimation techniques for the study of production function, and concluding remarks are provided in the fourth section.
2.1 Definition of Variables and Data Sources
Our sample of 15 MENA countries including (Algeria, Bahrain, Egypt, Iran, Israel, Jordan, Kuwait, Libya, Morocco, Oman, Qatar, Saudi Arabia, Syria, Tunisia and United Arab Emirates covering the period 1970 to 2010. To estimate the production function in MENA region, however, data on some key variables are not available for all the countries and hence our panel data is unbalanced. In addition details of the data are in the appendix.

Most data come from the World Bank, IMF, KLM, Penn World Tables 5.6 (PWT5.6) and our own calculations. From Barro and Lee (2012), we obtain educational attainment data average years of schooling for different category (primary, secondary and tertiary) which are available from 1960-2010 (Note 1).

2.2 Exogenous Growth Theory
A macroeconomic production function is a mathematical expression that describes a systematic relationship between inputs and output in an economy and the Cobb-Douglas is function that has been used extensively. This function plays an important role in the economic forecasts and policy analysis.

The neo-classical growth model is also known as the exogenous growth model or Solow growth model. The Solow model was developed by Nobel Prize winner Robert Solow. In Solow’s model, there are two factors of production: capital and labour. Technology is exogenous and represented by production function:

\[ Y = F(K, L) \]  \hspace{1cm} (1)

Where \( Y \) is output or real GDP, \( F \) the function of technology, \( K \) capital stock input, and \( L \) labour input.

A sustained increase in capital investment increases the growth rate only temporarily: the capital/labour ratio goes up. Steady-State growth path is reached when output, capital and labour are all growing at the same rate. These factors include, among others, technology level, quality of labour (human capital) which we use depending on our availability of data the government spending on health and education.

2.3 Measurement of Inputs
The neo-classical growth model is also known as the exogenous growth model or Solow growth model. In Solow’s model, there are two factors of production: capital and labour.

2.3.1 Measurement of Capital Stock \((K)\)
Of particular note is our use of a new dataset on capital stocks. The relevant reference concerning the construction of these capital stock estimates is Nehru and Dhareshwar (1993), and the dataset is available as part of the World Bank’s STARS databank and other sources as shown in Appendix B. investment at constant local prices and draws on additional data sources. They show that their capital stock estimates are positively correlated with other inputs.

2.3.2 Labour \((L)\)
Labour force is measured in millions and the series ranges from 1970 to 2010, and we used it in our measure as the growth of labour. All selected variables were in U.S dollar and in constant prices of 2005.

3. Education as Include in Calculation of Growth \((EDU)\)
As the present study confines itself to the growth of MENA region, thus, I shall concentrate on the secondary education category as a proxy for human capital development of the labour force in the economy.

3.1 Model Specification
This study examines the relationship between real growth of GDP and the growth of inputs factors (capital and Labour) using time series data for 15 MENA countries. The real GDP data was in real terms, with 2005 as the base year. Most of the three variables have unit root and non-stationary. The variables tend to show similar increasing or decreasing pattern over time. Hence, before proceeding with further analysis, the data must be tested for existence of unit roots using various tests available in the econometrics literature.

According to the literature above, generally the Cobb-Douglas function can be as following

\[ Y_t = AK^{\alpha}L^{1-\alpha} \]  \hspace{1cm} (2)

Where

\( Y \) is the real GDP; \( K \) is the capital input; \( L \) is the labour input; \( A \) is the technology.

3.2 Estimated
In our study we utilize three methods. First, we use cross section-data techniques to estimate the capital stock. Second, we relax this assumption and estimate the parameters of the production function separately for every
country based on identifying the long-run and short-run relationship between output and inputs by applying the Johansen Co-integration and Error Correction Model (ECM). Third, we conduct Impulse Response Function on our estimated to represent the behaviour of growth of real GDP, growth of capital and growth of labour.

3.3 Diagnostic Tests

As argued in the literature, we have to take into account the potential non-stationarity in the data; the following two step estimation strategy has been adopted:

First, test the three variables real GDP, stock of capital and labour in production function for presence of unit root.

3.3.1 Results of Unit Root Test

The results of Augmented Dicky-Fuller (ADF) test is presented in (Appendix D). From ADF test, we can conclude that \( \text{RGDP} \) on level is none stationary or integrated of order one I(1) for some countries, and the unit root of null hypothesis on the level can be rejected at 10 per cent or less only for three countries: Algeria, Bahrain and Syria. Also we take first difference; we fail to reject the null hypothesis for the same countries. For \( \ln K \), the unit-root hypothesis on the level or first difference can be rejected at 5 per cent for the following five countries: Algeria, United Arab Emirates, Saudi Arabia, Oman and Kuwait. For \( \ln t \), the unit-root of null hypothesis on the level and first difference can be rejected at 5 per cent for eight countries: Algeria, Bahrain, Egypt, Israel, Morocco, Oman, Saudi Arabia and United Arab Emirates.

3.3.2 Co-Integration Testing

The idea of using co-integration is that two or more variables may be regarded as defining a long-run equilibrium relationship if they move closely together in the together in the long run, even though they may drift apart in the short run. This long-run relationship is referred to as a co-integrating vector. Because there is a long-run relationship between the variables, a regression containing all the variables of a co-integrating vector will have a stationary error term, even if none of the variables taken alone is stationary. To this end our model for testing the long relationship as following:

\[
\ln Y_t = \alpha + \beta_1 \ln K_t + \beta_2 \ln L_t + \epsilon_t, \quad (3)
\]

In the case of the relationship among the \( \ln Y \), \( \ln K \) and \( \ln L \), we conclude that the null hypothesis of no co-integration is strongly rejected. The lag lengths are selected using AIC criteria.

3.3.3 Dummy Variables

In order to introduce regional dummy variables in the regressions to correct for the estimation bias due to the restrictive assumption of identical initial technologies for all sample countries, the complete sample of 15 countries is divided into two areas, Oil exporting countries and non-Oil exporting. We used OIL as Dummy variable for oil exporters based on the IMF classification of the countries taking 1 for countries whose fuel exports represent 50% or more of the total of exports during the period between 1984 and 1986, and 0 others.

3.3.4 Error Correction Mechanism (ECM)

The specifications use for estimating the growth effects of one or another growth enhancing variables, in both the cross country and country specific studies, need examination. Although most of these studies claim that they are estimating the permanent long-run growth effects, there is no distinction between the permanent long-run and the transitory short-run growth effects of variables. As we estimated the long-run relationship, also in this section the short-run is important for the policy makers especially of developing countries because of the affect which could be for more than five years and will have permanent level effects; see Rao and Cooray (2009) for more details. To this end, we specify and estimate an Error Correction Mechanism (ECM) appropriate as following:

\[
\Delta \ln Y_t = \alpha_1 + \sum \beta_{j1} \Delta \ln K_{t-j} + \sum \beta_{j2} \Delta \ln L_{t-j} + \gamma_1 EDU_{t-j} + \gamma_2 INF_{t-j} + \gamma_3 DUM_{t-j} + \eta_1 ECM_{t-j} + \epsilon_t \quad (4)
\]

3.3.5 Impulse Response Functions

Finally, we conduct Impulse Response Function (IFR) on our estimated. IFR is a practical way to visually represent the behaviour of RGDP (Y), Stock of Capital (K) and Labour (L) in response to the various shocks. Appendix (A) show figures of our IFR for 15 countries.
Table 1. Johansen’s Co-integration Test and LR test based on maximum Eigen value of stochastic matrix: variables: lnRGDP, lnK and lnL.

<table>
<thead>
<tr>
<th>Country</th>
<th>Hypothesis</th>
<th>Alternative</th>
<th>Eigen-value</th>
<th>λ – max</th>
<th>λ – Trace</th>
</tr>
</thead>
<tbody>
<tr>
<td>Israel</td>
<td>Var(3)</td>
<td>r = 0</td>
<td>0.996</td>
<td>229.925***</td>
<td>262.341***</td>
</tr>
<tr>
<td></td>
<td>LR estimated</td>
<td>lnRGDP = 26.911- 0.105lnK - 0.792 <em><strong>lnL+ 0.067</strong></em> t (0.415) (6.903) (11.203)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Jordan</td>
<td>Var(3)</td>
<td>r = 0</td>
<td>0.989</td>
<td>188.432***</td>
<td>219.106***</td>
</tr>
<tr>
<td></td>
<td>LR estimated</td>
<td>lnRGDP = 9.254+ 0.606<em><strong>lnK- 1.184</strong></em>lnL+0.067*** t (8.571) (8.725) (5.006)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Kuwait</td>
<td>Var(3)</td>
<td>r = 0</td>
<td>0.502</td>
<td>22.327***</td>
<td>24.640</td>
</tr>
<tr>
<td></td>
<td></td>
<td>r≤1</td>
<td>0.061</td>
<td>1.999</td>
<td>2.313</td>
</tr>
<tr>
<td></td>
<td></td>
<td>r≤2</td>
<td>0.009</td>
<td>0.314</td>
<td>0.314</td>
</tr>
<tr>
<td>Libya</td>
<td>Var(3)</td>
<td>r = 0</td>
<td>0.991</td>
<td>192.434***</td>
<td>213.549***</td>
</tr>
<tr>
<td></td>
<td>LR estimated</td>
<td>lnRGDP = 60.023 + 0.054<em>lnK + 2.768</em>**lnL (6.332) (1.686)</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**Note.** i) ***, ** and * implies significant at 1%, 5% and 10% level respectively.  
ii) Figures in parenthesis represent the t-statistics.

Table 2. Estimated co-efficient using VECM from 1970-2010

<table>
<thead>
<tr>
<th>Dependent variable = Δ ln Y</th>
<th>Algeria</th>
<th>Bahrain</th>
<th>Egypt</th>
<th>Iran</th>
</tr>
</thead>
<tbody>
<tr>
<td>ECM r-1</td>
<td>0.241***</td>
<td>-0.308***</td>
<td>-0.002***</td>
<td>-0.362***</td>
</tr>
<tr>
<td>(3.852)</td>
<td>(41.363)</td>
<td>(13.085)</td>
<td>(18.661)</td>
<td></td>
</tr>
<tr>
<td>Δ ln Y r-1</td>
<td>-0.211</td>
<td>0.537*</td>
<td>0.230</td>
<td>0.352*</td>
</tr>
<tr>
<td>(-1.250)</td>
<td>(1.880)</td>
<td>(1.320)</td>
<td>(1.673)</td>
<td></td>
</tr>
<tr>
<td>Δ ln K r-1</td>
<td>1.262**</td>
<td>0.213</td>
<td>0.731***</td>
<td>1.620**</td>
</tr>
<tr>
<td>(2.914)</td>
<td>(0.417)</td>
<td>(3.280)</td>
<td>(1.915)</td>
<td></td>
</tr>
<tr>
<td>Δ ln L r-1</td>
<td>-1.113</td>
<td>-0.514</td>
<td>0.081**</td>
<td>-1.356***</td>
</tr>
<tr>
<td>(-0.844)</td>
<td>(-1.503)</td>
<td>(2.010)</td>
<td>(-3.122)</td>
<td></td>
</tr>
</tbody>
</table>

**Exogenous variables**

<table>
<thead>
<tr>
<th></th>
<th>Algeria</th>
<th>Bahrain</th>
<th>Egypt</th>
<th>Iran</th>
</tr>
</thead>
<tbody>
<tr>
<td>DUM</td>
<td>0.005</td>
<td>-0.031</td>
<td>0.011</td>
<td>-0.006</td>
</tr>
<tr>
<td>(0.374)</td>
<td>(-0.836)</td>
<td>(1.135)</td>
<td>(0.239)</td>
<td></td>
</tr>
<tr>
<td>INF</td>
<td>0.002</td>
<td>-0.002</td>
<td>-0.001</td>
<td>-0.004**</td>
</tr>
<tr>
<td>(1.041)</td>
<td>(-0.566)</td>
<td>(-1.129)</td>
<td>(-2.539)</td>
<td></td>
</tr>
<tr>
<td>EDU</td>
<td>0.042***</td>
<td>0.157***</td>
<td>0.005*</td>
<td>0.109***</td>
</tr>
<tr>
<td>(3.484)</td>
<td>(19.685)</td>
<td>(1.630)</td>
<td>(18.328)</td>
<td></td>
</tr>
<tr>
<td>Constant</td>
<td>-0.257***</td>
<td>-1.063***</td>
<td>0.013</td>
<td>-0.497***</td>
</tr>
<tr>
<td>(2.444)</td>
<td>(-18.095)</td>
<td>(0.674)</td>
<td>(-11.881)</td>
<td></td>
</tr>
<tr>
<td>R²</td>
<td>0.638</td>
<td>0.994</td>
<td>0.896</td>
<td>0.960</td>
</tr>
<tr>
<td>Adj. R²</td>
<td>0.504</td>
<td>0.989</td>
<td>0.862</td>
<td>0.941</td>
</tr>
<tr>
<td>Standard error</td>
<td>0.019</td>
<td>0.052</td>
<td>0.020</td>
<td>0.055</td>
</tr>
<tr>
<td>AIC</td>
<td>-4.864</td>
<td>-2.771</td>
<td>-4.713</td>
<td>-2.694</td>
</tr>
<tr>
<td>F-stat</td>
<td>4.765**</td>
<td>245.618***</td>
<td>25.934***</td>
<td>50.403***</td>
</tr>
</tbody>
</table>

**Note.** i) ***, ** and * implies significant at 1%, 5% and 10% level respectively.  
ii) Figures in parenthesis represent the t-statistics.
In this chapter the above objective is attained in the following way: first of all, we have estimated the initial relationship, and Error Correction Model for short run relationship, and Error Correction Model for long run by taking in our consideration the structural break. Both estimations provide the most reliable results for some countries after we include dummy variable for some countries where the growth of population in some countries such as Egypt, Jordan and Tunisia.

4. Concluding Remarks

The overall growth performance of the MENA countries has been both mixed and characterized by a higher degree of volatility in comparison with oil exporter countries and non-oil countries. Several sources of uncertainty in the region can explain this volatility. These include, among others, fluctuations in world oil prices, investment (capital flows) and factors contributing the socio-political instability in the region such as civil wars and regional conflicts such as Golf War and Iranian revolution.

The analysis covers a sample of 15 MENA countries of which (including MENA oil countries, and non-oil MENA countries) had complete data for all variables. The objective of this chapter, as mentioned in the introduction, is first to see the main source of growth in the North Africa and Middle-East countries by applying Cobb-Douglas specification, and second to check for robustness of any relationship that may exist in the short and long-run by applying Johansen Co-integration, Error Correction Model (ECM) methods, and Impulse Response Function (IRF). That is likely to persist in these three variables $\Delta \ln Y$, $\Delta \ln K$ and $\Delta \ln L$. In this chapter the above objective is attained in the following way: first of all, we have estimated the initial capital stock by applying several approaches to get a series of capital ($K$). Also, we test for stationarity by applying conventional unit root test (ADF) without considering the existence of potential structural break, then we test for unit root in the presence of potential structural break by applying different approaches (DF-GLS and KPSS) in order to examine the stationarity of the data with unknown structural break. A variety of specifications are estimated, Johansen Co-integration estimation for a long-run relationship, and Error Correction Model for short-run relationship by taking in our consideration the structural break. Both estimations provide the most reliable results for some countries after we include dummy variable for some countries where the oil prices can affect the growth of real GDP.

The variables selected in this chapter for all of these different estimators are summarised in Table 1, 2 and 3. The main conclusion is that the growth of $K$ in some oil MENA countries generally grows faster than the growth of $L$ in some countries. Contrarily, in non-oil countries labour is a quit grows faster than capital. That is of course due to some factors such as increase of the growth of population in some countries such as Egypt, Jordan and Tunisia. I conclude from my results that some MENA countries like Qatar, Saudi Arabia and United Arab Emirates the...
aggregate production function does not appear to be Cobb-Douglas. This relationship remains robust even after allowing the (IRF) to be jointly determined in a system. The estimated of the production function is for a long-run and short-run; however, these estimates are in line with the estimated in previous studies as mentioned in the literature. The signs of the estimated of growth of $K$ and growth of $L$ with respect to real GDP has been interpreted as follows: firstly, in the long-run the increases in $\Delta\ln K$ in some countries will lead to increase in output, simply because more investment will lead to increase of growth of RGDP. A similar result is reported by Adams and Felipe (2005), though the coefficient there was not significant. Secondly, the short-run relationship as reported in table 2. It shows the results of the Error Correction Mechanism (ECM) term, and it represents the speed of adjustment back to the long-run relationship among the variables for 15 countries under study for real GDP growth $\Delta\ln RGDP$. The estimated co-efficient shows the immediate impact of inputs $\Delta\ln k, \Delta\ln l$ and $inf, edu$ as exogenous variables on $\Delta\ln RGDP$. The ECM terms are significant for our entire sample.

In the short-run increase in education measured by secondary schooling years, is associated with higher increase of growth of real GDP, because this improves the skills opportunities of employees in the future. However, an increase in education leads to increase in the output.

References


**Note**

Note 1. Schooling data from Barro and Lee(2010) are available only every five years, so we can use linear interpolation in between.

**Appendix A. Impulse Response Functions**

![Response of DLNK to DLNK](image1)

![Response of DLNY to DLNY](image2)

![Response of DLNK to DLNY](image3)

![Response of DLNK to DLNY](image4)

![Response of DLNY to DLNY](image5)

![Response of DLNK to DLNY](image6)

![Response of DLNY to DLNY](image7)

![Response of DLNK to DLNY](image8)
Appendix B. Critical value of different unit root test

<table>
<thead>
<tr>
<th></th>
<th>ADF</th>
<th>DF-GLS</th>
<th>KPSS</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>C</td>
<td>C &amp; T</td>
<td>C</td>
</tr>
<tr>
<td>1% level</td>
<td>-3.621</td>
<td>-4.147</td>
<td>-2.618</td>
</tr>
<tr>
<td>5% level</td>
<td>-2.943</td>
<td>-3.517</td>
<td>-1.948</td>
</tr>
<tr>
<td>10% level</td>
<td>-2.610</td>
<td>-3.185</td>
<td>-1.612</td>
</tr>
</tbody>
</table>

Source: Eviews 7 calculation.

Note. The lag length of ADF and KPSS a test are AIC, but for DF-GLS is SIC.

Unit root test include intercept (C) and trend (T), but for KPSS test we report constant only (C).

Appendix C. Definition of variables and sources: world Bank, IMF, KILM, Penn World Bank, UN and Barro-Lee data

<table>
<thead>
<tr>
<th>Variables</th>
<th>Definition</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>RGDP (Y)</td>
<td>Real Gross Domestic Product. GDP at purchaser’s prices is sum of gross value added by all resident producers in the economy plus any product taxes and minus any subsidies not included in the value of products. The value in constant US 2000 U.S dollars.</td>
<td>World Development Indicators (WDI) 2010</td>
</tr>
<tr>
<td>CPI</td>
<td>Consumer price at constant year of 2005</td>
<td>World Development Indicators, 2010</td>
</tr>
<tr>
<td>INF</td>
<td>Inflation rate</td>
<td>World Bank national account data (World Development Indicators, 2010)</td>
</tr>
<tr>
<td>INV(GFCF)</td>
<td>Real investment From (IRAT*RGDP)/100</td>
<td>World Bank (World Development Indicators, 2010)</td>
</tr>
<tr>
<td>K</td>
<td>Capital Stock; derived using perpetual inventory method (depreciation =0.05) \n[ K_t = (1 - \delta) K_{t-1} + I_t ]</td>
<td>World development indicators(WDI) 2010</td>
</tr>
<tr>
<td>Dummy</td>
<td>This is oil dummy variables take a value of 0 for oil MENA countries when there are changes in oil prices and one otherwise.</td>
<td>Computed by author</td>
</tr>
<tr>
<td>EDU</td>
<td>Average years of secondary schooling among population aged over 25 years</td>
<td>Barro and Lee (2010) database</td>
</tr>
<tr>
<td>K</td>
<td>Capital stock; derived using perpetual inventory method \n[ K_t = K_n \times 0.95 + I_t ] \n[ I_t ] is real gross domestic fixed investment (the depreciation is 0.05)</td>
<td>International Monetary Fund (IMF) database, 2010</td>
</tr>
</tbody>
</table>

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