Constructing Progress Maps of Digital Technology for Diagnosing Mathematical Proficiency

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Abstract

This research aims to construct and validate progress maps of digital technology for diagnosing the multidimensional mathematical proficiency (MP) in Number and Algebra for Grade 7 students utilizing the Construct Modeling Approach. Researchers employed four building blocks as follows. Firstly, researchers developed the progress maps as an assessment framework of multidimensional MP. This is followed by creating the test for diagnosing MP. Next, researchers assigned scoring criteria and created the transition points of students’ MP levels. Finally, researchers validated the quality of the progress maps through empirical evidence. A total sample 1,500 Grade 7 students was used to support the validity and reliability evidence of the progress maps through the Wright Map using Multidimensional Random Coefficients Multinomial Logit Model. Results revealed that there were two dimensions of progress maps, namely mathematical procedures (MAP) and structure of learning outcome (SLO), and the researchers investigated three strands of validity evidence, namely test content, response processes, and internal structure. The reliability values in the MAP and SLO were 0.84 and 0.80 respectively. Finally, the Grade 7 students were mainly found to be at level-2 in the MAP dimension (44.95%) and the SLO dimension (61.57%). The experts’ evaluation results showed that the digital technology that was developed at the “most appropriate” quality levels in terms of usefulness, suitability, and accuracy, and at the “very appropriate” for the feasibility aspect, and hence is successfully contributing to the clarification of learning goals, to support for student-centered instruction, and that it is helpful in improving in teacher professional development.

Keywords: mathematical procedures, multidimensional mathematical proficiency, number and algebra, progress maps, structure of learning outcome

1. Introduction

Mathematics is a form of practical knowledge in our daily life which is not only a fundamental discipline but also a foundation for many other scientific disciplines and thus it plays a significant role in stimulating students' learning (Huang, Huang, & Wu, 2014). Since we are living in an era of accelerating change in society, particularly due to technological development, students have to be prepared with sufficient mathematical proficiency (MP) in terms of skills and competencies needed for work and life in the 21st Century (Redecker & Johannessen, 2014). MP is defined as a student’s ability to explore, conjecture, and reason logically in cognitive processes and to understand how to solve mathematics problems that is to, apply, and adopt appropriate strategies to solve the problems, and reflect on the process used to solve the problems (Junpeng, Inprasitha, & Wilson, 2018).

The United States National Research Council (2001) identified five strands of MP consisting of conceptual understanding, procedural fluency, strategic competence, adaptive reasoning, and productive disposition and their definitions as follows. **Conceptual understanding** refers to the integrated and functional grasp of mathematical ideas which enables students to learn new ideas by connecting those ideas to what they already know. The **procedural fluency** is defined as the skill in carrying out procedures flexibly, accurately, efficiently, and appropriately. **Strategic competence** is the ability to formulate, represent, and solve mathematical problems.
Adaptive reasoning means the capacity for logical thought, reflection, explanation, and justification. Productive disposition is the inclination to see mathematics as sensible, useful, and worthwhile, coupled with a belief in diligence and one’s efficacy.

MP requires the students not only be able to recall conceptual knowledge but also use this knowledge to engage in practices such as developing inquiries, creating explanations and interpreting data (OECD, 2016). There are a few existing diagnostic tools such as ALEKS, Carnegie Learning’s Cognitive Tutors, Ms. Linkquist, and ActiveMath designed to diagnose students’ mathematics problem-solving abilities. However, these tools differ in terms of the measurement technique employed, and perhaps more importantly on the local level of the diagnosis there is a wide range, for example from analyzing specific problem-solving steps to a global level, such as inferring mastery status of general MPs (Shute & Underwood, 2006).

Through enhanced digital technology in education, teachers have begun to realize the benefits of technology in making drastic changes to their instruction, assessments, and even the physical make-up of their classrooms, and are doing so at a much faster rate than expected (Newman, 2017). The current educational sector is becoming more competitive, and hence digital technologies are becoming a necessary means of survival: the new digital educational environment requires teachers to adapt and adopt digital technologies, methodologies, and mindsets (O’Brien, n.d.). Digital assessment is one of the effective ways to diagnose MP by improving assessment across a range of contexts and purposes (Drasgow, 2016; Gane, Zaidi, & Pellegrino, 2018).

One of the greatest challenges in Grade 7 mathematics education is serving the diverse preparation and students’ needs within a framework that is both driven by research yet simplifies the management task. This is because teachers and students must have a simple, transparent, and constant means to guide and assess learning mathematics (Junpeng et al., 2018). As a result, researchers aimed to create a digital learning system focusing on dynamic assessment, grounded in research on learning trajectories around great ideas, and designed to inform instructional practices within a competency-based and personalization-based model of school change to diagnose and improve students’ MP. On this line of reasoning, researchers aimed to construct and validate the progress maps of digital technology for diagnosing multidimensional MP in Number and Algebra to the Grade 7 students utilizing Construct Modeling Approach.

2. Literature Review

2.1 A Developmental Perspective on Student Learning

MP is defined as the mathematical process of applying mathematical knowledge. Since mathematics is considered as fundamental to a child’s development and communication in later life, basic numeracy skills are essential to assist them to be a competent adult with high achievement (Papadakis, Kalogiannakis, & Zaranis, 2018). Several cycles of piloting and revising the tasks for assessing MP were conducted. This is predominantly accurate for open-response questions where students are requested to produce and transcribe the answer, employing higher-order thinking, provoking the measured MP, and enlightening the MP process through the practice of two dimensions, namely mathematical procedures (MAP) (Junpeng et al., 2018) and structure of learning outcome (SLO) (Biggs & Collis, 1982).

The Structure of the Observed Learning Outcome (SOLO taxonomy) is a model used to identify, describe or explain the level of understanding to determine the quality level of students’ learning results and can be used to measure the SLO. Biggs and Collis (1982) proposed the concept of conceptual structure into five levels, namely pre-structural, uni-structural, multi-structural, relational, and extended abstract. The pre-structural level is where students do not understand the true purpose and still use simple methods to understand the content. They cannot create concepts and still have misunderstandings in their mathematical thinking. The unistructural level refers to response where the student’s focus is related to only one view of the mathematical situation. They can identify things that they learn by memorizing, such as identifying names, remembering, and following simple instructions. The multi-structural level refers to a response where the students’ focus is on many perspectives and they can connect complex concepts, explain, and describe each section. The relational level is the integration of various relationships together. They can analyze, compare, identify differences, explain the logical relationship and apply what they learned but they still cannot conclude abstract knowledge. The extended abstract refers to the integration of the relationships. Students can create an advanced abstract concept or create a new theory and make a conclusion based on the concepts that they learn.

2.2 Mathematical Proficiency Assessment

Junpeng et al. (2018) developed an assessment system using construct modeling to assess students’ MP in mathematics problems-solving in terms of their 3-D process-oriented thinking, namely mathematical procedures...
(MAP), mathematical strategies (MAS), and mathematical reasoning (MAR). Their findings showed that the abilities of students in these three dimensions correlated between 0.86 and 0.89.

A successful progress map displays what is to be measured or assessed in terms general enough to be interpretable across a curriculum but specific enough to guide MP item development. When the students’ responses are linked to the progress map, then it can be determined what is the students’ level of learning. The progress map is one model of how assessment can be integrated with diagnosis and instruction (Watson & Ohtani, 2015). Figure 1 shows the progress maps of mathematical procedures, mathematical strategies, and mathematical reasoning to assess students’ abilities in solving mathematics problems (Junpeng et al., 2018).

![Progress Map Diagram]

Figure 1. Framework for assessing mathematics problem-solving MP

In this study, we will be focusing on the MAP dimension among these three, but also on SLO.

2.3 Multidimensional Response Test Model

Item Response Theory is a measurement approach base on a model of the relationship between the students’ ability and item difficulty. Some examples are the One-Parameter Logistic Model (Rasch Model), the Two Parameter Logistic Model, and the Three-Parameter Logistic Model (Embretson & Reise, 2000).

The MRCMLM (Adams, Wilson, & Wang, 1997) is an extended Rasch model that is more flexible allowing for the specification of a large number of multidimensional item response models. This model uses design matrices to specify the relationship between responses to the items and structural parameters assumed for a given measurement situation. For this project, the parameters in these models were estimated using ACER ConQuest (Wu, Adam, Wilson, & Haldane, 2007). The model fit, reliability and item fit comparisons provide the reliability and validity evidence for selecting the assessment framework with the flexibility and appropriateness for diagnosing in a real-world context.

A Wright map is the distribution of item difficulty, the students’ ability, and their MP level in terms of the probability of answering correctly each item of the examination. This probability is represented by the distance between the student and the examination as reflected in the Rasch Model. The test is considered as difficult if the difficulty level of most of the items is above the mean of the students (Baker & Kim, 2017).

2.4 Past Research Review

Huang et al. (2014) adopted an Input-Process-Outcome digital game-based learning system with a diagnostic mechanism strategy for a primary school mathematics course. Their research results showed that students can be engaged in mathematics learning through a digital game-based learning system and this leads to positive motivation. Besides, their research results imply that teachers should integrate a motivating game model into mathematics learning and provide a diagnostic mechanism that can enhance students’ interest and reduce the
anxiety of learning mathematics. Finally, Huang et al. (2014) concluded that learning motivation and learning performance are enhanced when anxiety is mitigated.

Ketterlin-Geller and Yovanoff (2009) found that diagnosis is an integral part of instructional decision-making as it can be the bridge between identification of students who may be at-risk for failure if the instructional delivery is not designed carefully with diagnostic assessments. This is because diagnostic assessments can provide valuable information about students’ persistent misconceptions in the targeted domain. Ketterlin-Geller and Yovanoff (2009) pointed out that cognitive diagnostic assessments are an emerging solution to provide detailed and precise information about students’ thinking that is needed to provide appropriate educational opportunities for students who struggle in mathematics.

Faber, Luyten and Visscher (2017) examined the effects of a digital formative assessment tool on mathematics achievement and motivation in Grade 3 primary education. A total of 79 schools and 1808 students participated in their research. The experimental schools used a digital formative assessment tool while control schools used their regular teaching methods and materials. The digital tool used in their research consisted of students' feedback, feedback to teachers, and adaptive assignments. The collected data were standardized achievement pretests and posttests, a student motivation survey, classroom observations, and students’ log files. Multilevel analysis showed that there are positive effects of the digital formative assessment tool towards students’ achievement and motivation. Furthermore, achievement effects were found to be greater for high-performing students.

Gane et al. (2018) illustrated the challenges that were associated with the assessment of multidimensional learning to diagnose science proficiency and the benefits provided by technology. They framed the assessment development as an evidence-centered design process and illustrated it by using cases drawn from middle school science. Then they turned to ways in which assessment systems need to evolve to expand the scope of what the students can do in the creation and use of valid, reliable, and equitable assessments of complex and multidimensional learning. They concluded that technology-based assessment systems with an emphasis on measuring what matters versus measuring what is easy are efficacious, since what they choose to assess will become the focus of instruction. They also suggested that investment in the development, validation, and deployment of technology-based assessments that reflect the multidimensional competencies identified by contemporary research and theory will form major advances in assessment policy and practice.

Chanayota and Junpeng (2016) investigated of mathematical reasoning skills in the Theorem Pythagorean topic for Grade 5 students. Cronbach’s alpha for the test was 0.74. Their findings showed that students have different levels of mathematical reasoning skills. The majority of the students were at the level of strategic thinking skills.

3. Method

Researchers employed the construct modeling approval based on Wilson’s (2005) developmental assessment ideas that embed pedagogy and curriculum in the design of diagnostic tasks and so-called the Berkeley Evaluation and Assessment Research (BEAR) assessment system (BAS). Wilson and Sloane (2000) proposed the four building blocks as the components of the assessment system, namely progress maps; design of tasks; outcome space, and measurement model (as represented by the Wright map). BAS is conducted under four principles as follows: (i) A developmental perspective of students’ learning; (ii) the link between instruction and assessment; (iii) teacher management of classroom instruction and assessment, and (vi) generation of high-quality evidence.

3.1 Research Design and Sample

The study employed a research and development design to develop a framework to assess Grade 7 students’ MP levels. The population of the study is all the Grade 7 students in secondary schools located in the northeastern region of Thailand. The total population was 136,063 students in the year 2017. The stratified random sampling technique was employed, and the sample size required was 1,500. Moreover, the required sample size for estimation of item parameters in the multidimensional model of the Rasch-family models is 400 to 500 to provide accurate parameter estimates (Custer, 2015; Jiang, Wang, & Weiss, 2016).

A total of 30 Grade 7 students from three different proficiency levels were selected as the pre-pilot group for creating the progress maps. There were two groups of examinees used to validate the progress maps, namely 200 and 1,500 examinees who involved in pilot study and actual study respectively. The role of the evidence from the 200 examinees was to explore the quality of levels and descriptions in each progress map with link test items and scoring guide through the Wright Map using the Rasch model. The evidence from the 1,500 examinees supported the validity and reliability argument about the progress maps, again through the Wright Map.
3.2 Research Procedure

3.2.1 Progress Maps

Researchers developed the assessment framework and diagnostic tasks with teachers and educators to identify the specific assessment objectives. The Grade 7 mathematics education core curriculum of Thailand (Ministry of Education, 2017) has three big strands, namely (i) number and algebra (ii) measurement and geometry, and (iii) statistics and probability. This assessment design focused on number and algebra which consisted of two learning standards that relate to understanding of diverse methods of presenting numbers and operations in the real life and applying algebraic expressions, equation, and other mathematical models to represent various situations as shown in Figure 2. The MAP and SLO are ‘progress maps’, used to diagnose multidimensional proficiencies in these learning strands.

Figure 2. Three big strands and six learning standards of Grade 7 mathematics curriculum

3.2.2 Design of Tasks (A Match between Instruction and Assessment)

All MP tasks are created according to the core curriculum. Therefore, the tasks were re-designed according to teachers and content experts’ feedback as well as an initial empirical analysis of the pilot testing, using the Wright map, item fit, and step fit for validation purposes, and the internal consistency and split-half reliability coefficients for reliability information. Based on the pilot testing results, researchers deleted those tasks that overlapped the content knowledge between items and also some tasks were found inappropriate for Grade 7 students. Subsequently, a mixed format was developed including open-ended questions and selected-response test items which consisted of 18 items—11 and 7 items of MAP and SLO dimensions, respectively.

3.2.3 Outcome Space (Teacher Management and Responsibility)

A specific scoring guide was used to assess students’ MAP and SLO as the two MP dimensions. The scores of this scoring guide ranged from 0 to 4 and 0 to 3 respectively, indicating inappropriate, partly appropriate, most appropriate, and beyond proficiency. The scoring guide was utilized during the whole class for all assessment connecting to any of the dimensions. Table 1 shows the scoring guide of the MAP and SLO dimensions which
consisted of five and four proficiency levels respectively (i.e., see the Number and Algebra box in Figure 2).

Table 1. Scoring guide of proficiency levels for diagnosing students’ ability in MAP and SLO dimensions

<table>
<thead>
<tr>
<th>Level</th>
<th>Score</th>
<th>Learning Progress Level of MAP</th>
<th>Diagnostic Description</th>
<th>Level</th>
<th>Score</th>
<th>Learning Progress Level of SLO</th>
<th>Diagnostic Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>4</td>
<td>Strategic/Extended Thinking</td>
<td>- Student is able to show a variety of complex and appropriate solutions</td>
<td>4</td>
<td>3</td>
<td>Relational/Extended Abstract</td>
<td>- Student can solve problems in each situation and create a relationship of problem situations</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>- Student is able to expand the original knowledge to new knowledge for finding answers</td>
<td></td>
<td></td>
<td></td>
<td>- Student can use concepts to connect and can summarize references as abstract knowledge.</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>- Student is able to create his own ideas</td>
<td></td>
<td></td>
<td></td>
<td>- Student can create knowledge from his own ideas.</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>- Student can choose appropriate strategies and concepts to solve the problems.</td>
<td></td>
<td></td>
<td></td>
<td>- Student can solve the problems in each situation but student cannot associate the relationships of the each situation together.</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>- Student can display the relationship of numbers and write them in general as a mathematical model.</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>3</td>
<td>Simple Skills/Concept</td>
<td>- Student can apply basic mathematical knowledge to solve more complex problems through the process or method.</td>
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<td></td>
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<td></td>
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<tr>
<td></td>
<td></td>
<td></td>
<td>- Student can solve the problems to reflect that he has the knowledge and understanding of principles used.</td>
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<tr>
<td></td>
<td></td>
<td></td>
<td>- Student can explain using the mathematical symbols appropriately.</td>
<td></td>
<td></td>
<td>Multi-structural</td>
<td>- Student can solve the problems in a manner like an example but when adding conditions, student cannot connect the concept to solve the problems.</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>- Student can use the method of addition, subtraction, multiplication, and division but cannot be combined all together.</td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>2</td>
<td>Basic memory/Reproduction</td>
<td>- Student can apply the basic knowledge to solve the simple or familiar mathematical problems.</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>- Student is able to write explanations of the concepts but can not explain in the form of mathematical symbols.</td>
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<tr>
<td></td>
<td></td>
<td></td>
<td>- Student lacks of knowledge and understanding about applying mathematical principles to solve problems and it is impossible for him to solve problems at a higher level.</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>1</td>
<td>Unrecalled Memory</td>
<td>- Student can not use basic knowledge or important knowledge in the number and algebra to use in image analysis and also cannot identify the relationship of that image.</td>
<td></td>
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<tr>
<td></td>
<td></td>
<td></td>
<td>- Student can find the answer but cannot explain an appropriate method to answer the question.</td>
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<tr>
<td></td>
<td></td>
<td></td>
<td>- Student can not extend the solution to this issue at a higher level</td>
<td></td>
<td></td>
<td>Pre-structural</td>
<td>- Student lacks the skills in interpretation of questions/problems/situations.</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>- Student is unable to answer or answer unrelatedly.</td>
<td></td>
<td></td>
<td></td>
<td>- Students can not create the concept of number and algebra.</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>Non-response/Irrelavance</td>
<td>- Student is unable to answer or answer unrelatedly.</td>
<td></td>
<td></td>
<td></td>
<td>- Student is unable to link the algebraic concepts.</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>- Student is unable to answer or answer unrelatedly.</td>
<td></td>
<td></td>
<td></td>
<td>- Student has misconception in number and algebra.</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>- Student is unable to answer or answer unrelatedly.</td>
<td></td>
<td></td>
<td></td>
<td>- Student is unable to answer or answer unrelatedly.</td>
</tr>
</tbody>
</table>

3.2.4 Measurement Model (Generating Quality Evidence)

This study employed the MRCMLM (Adams, Wilson, & Wang, 1997) which is the family of Rasch Model (Rasch, 1960) to investigate a sound progress maps for diagnosing MP. MRCMLM is a measurement tool that enables researchers to relate the modelling of items in multidimensional proficiencies, estimate of the students’ proficiency parameter, and set the transition points for diagnosing student’s MP level in each dimension. The parameters in these models are estimated using ACER ConQuest version 2.0 (Wu, Adam, Wilson, & Haldane, 2007). The Wright map provide the reliability and validity for validating the quality of the progress map in each dimension.
3.3 Evaluation Assessment on Digital Diagnostic MP Tool

Researchers adapted the concepts of Stufflebeam (as presented in Kanjanawasi, 2011) to evaluate the quality of the digital diagnostic MP tool in four aspects, namely usefulness, feasibility, suitability, and accuracy. *Usefulness* is measured according to the benefits of the diagnostic MP tool to serve the needs of the students on time and have a good effect on using it. *Feasibility* is to ensure the consistency of the reality for practical, acceptable, economical, and cost-effective situations. *Suitability* is to ensure that the system is appropriate for its quality or state of being and will ultimately depend on the needs of the users. *Accuracy* is defined as the degree to which the result of a measurement or specification conforms to the correct value or a standard of precision.

The final phase of this research was to evaluate the usefulness, feasibility, suitability, and accuracy of the digital technology assessment system to diagnose MP by 10 experts after digital technology has been successfully implemented. A five-point Likert scale evaluation form was used as an instrument to gauge the experts’ views ranged from minimal, less, medium, extreme, to most appropriate levels. The five appropriateness levels were interpreted according to the average score as shown in Table 2.

<table>
<thead>
<tr>
<th>Mean Score Range</th>
<th>Interpretation</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.50–5.00</td>
<td>Most appropriate</td>
</tr>
<tr>
<td>3.50–4.49</td>
<td>Very appropriate</td>
</tr>
<tr>
<td>2.50–3.49</td>
<td>Medium appropriate</td>
</tr>
<tr>
<td>1.50–2.49</td>
<td>Less appropriate</td>
</tr>
<tr>
<td>1.00–1.49</td>
<td>Minimal appropriate</td>
</tr>
</tbody>
</table>

4. Results

The results of this research are presented in line with the research aim indicated above. The initial result was the development of the progress maps as an assessment framework of multidimensional MP. This is followed by creating the test for diagnosing MP. Next, the scoring criteria were assigned to measure Grade 7 students’ MP levels. Finally, a Heuristic evaluation of the quality of digital technology in terms of its usefulness, feasibility, suitability, and accuracy by 10 experts is performed.

4.1 Development of Progress Maps of Digital Technology for Diagnosing MP

Researchers employed a construct modelling approach to access Grade 7 students’ multidimensional MP on number and algebra in terms of MAP and SLO. According to the assessment results, researchers found that there were two learning standards, namely M1.1 and M1.2. These learning standards had two progress maps (see Figure 3). The MAP progress map had five levels, namely non-response/irrelevance, unrecalled memory, basic memory/reproduction, simple skills/concept, and strategic/extended thinking levels (see Figure 3). Besides, the EAP/PV reliability value was 0.84 and Cronbach’s Alpha coefficient was 0.85, thus it was concluded as having acceptable reliability. Results imply that the test was found to be suitable for the Grade 7 students and they were at a moderate level of MAP dimension of MP.

On the other hand, the results of the SLO progress map showed that there were four levels of SLO, namely pre-structural, uni-structural, multi structural, and relational/extended abstract levels (see Figure 3). The EAP/PV reliability value was 0.80 and Cronbach’s Alpha coefficient was 0.85, thus it was concluded as having acceptable reliability. Once again, results of the SLO dimension imply that the test was found to be suitable for the Grade 7 students and they were at a moderate level of SLO dimension of MP. Besides, there were three strands of validity evidence found, namely test content, response processes, and internal structure being identified in the progress maps through the Wright map (see Figure 4).
4.2 Scoring Criteria and Determination of Grade 7 Students’ Multidimensional MP

The scoring criteria of the MAP dimension consisted of five levels, ranged from 0 to 4 points while the scoring criteria of the SLO dimension were comprised of four levels, ranged from 0 to 3 points. As a result, the intersection of MAP dimension’s transition point from levels 1 to 5 was found to be -0.24, 0.49, 1.11, and 1.67 respectively. On the other hand, the intersection of the SLO dimension’s transition point from levels 1 to 4 was found to be -0.63, 1.18, and 1.66 respectively. Finally, the Grade 7 students were found at level-2 in both multidimensional MP, namely MAP dimension (44.95%) and SLO dimension (61.57%). Figure 4 shows the results of the scoring of Grade 7 students and how researchers determined their multidimensional MP.
4.3 Heuristic Evaluation Results

The Heuristic evaluation results on the quality of digital technology in terms of its usefulness, feasibility, suitability, and accuracy were evaluated by 10 experts. Results of the Heuristic evaluation showed that the digital technology system was at most appropriate levels in terms of its accuracy, usefulness, and suitability except feasibility. The feasibility of digital technology was at the “very appropriate” level. The highest average was the accuracy of digital technology ($\bar{X}=4.67, SD=0.33$). This implies that this digital technology is able to identify the objective of the diagnostic assessment accurately ($\bar{X}=5.00, SD=0.00$), the evaluation process of the diagnostic assessment system is accurate ($\bar{X}=4.40, SD=0.49$), and the report of the reflection data is accurate according to the actual ability of the students ($\bar{X}=4.60, SD=0.49$).

This is followed by the suitability of digital technology which was at the “most appropriate” level ($\bar{X}=4.64, SD=0.44$). This implies that the assessment process, the completeness of the evaluation report, and the assessment system is consistent with the assessment guidelines ($\bar{X}=4.80, SD=0.40$). Besides, there is a clear agreement before the assessment is conducted as well as the scope of the assessment content ($\bar{X}=4.40, SD=0.49$). Next, the average score from the experts showed that usefulness of digital technology was at the “most appropriate” level ($\bar{X}=4.60, SD=0.46$). This implies that digital technology can respond to the needs of the students, students’ feedback can be utilized to diagnose MP, and can prepare students to improve their learning outcomes.

The feasibility aspect had the lowest average mean ($\bar{X}=4.26, SD=0.13$) if compared to the other three aspects of quality. Therefore, the feasibility of digital technology was found at a “very appropriate” level. This implies that the digital technology can be used to assess the ability of students and can be used by teachers in developing learning management and student development ($\bar{X}=5.00, SD=0.00$), the result of the evaluation is appropriate ($\bar{X}=4.00, SD=0.00$), and the system process and procedure is practical ($\bar{X}=3.80, SD=0.40$). Table 3 shows the results of the heuristic evaluation.
Table 3. Heuristic evaluation

<table>
<thead>
<tr>
<th>Quality Aspect</th>
<th>Average Score</th>
<th>Standard Deviation</th>
<th>Appropriate Level</th>
</tr>
</thead>
<tbody>
<tr>
<td>Accuracy</td>
<td>4.67</td>
<td>0.33</td>
<td>Most appropriate</td>
</tr>
<tr>
<td>Suitability</td>
<td>4.64</td>
<td>0.44</td>
<td>Most appropriate</td>
</tr>
<tr>
<td>Usefulness</td>
<td>4.60</td>
<td>0.46</td>
<td>Most appropriate</td>
</tr>
<tr>
<td>Feasibility</td>
<td>4.26</td>
<td>0.13</td>
<td>Very appropriate</td>
</tr>
</tbody>
</table>

5. Discussion and Conclusion

The key results of this research are the progress maps for the digital diagnostic tool to diagnose Grade 7 students’ MP in terms of MAP and SLO dimensions. Besides, expert opinion found that this digital technology tool is at the “most appropriate” level in terms of its accuracy, suitability, and usefulness and “very appropriate” in its feasibility aspect. As a result, this digital technology has been found to be not only timely, accurate, and relevant to teaching but also very informative on student progress in a systematic manner, precise, and can be taken multiple times. In addition, results revealed that the progress maps help give a clear vision of the learning goals, identification of big strand, including two learning standards which are in line with Thailand National Core Standards of Grade 7 mathematics curriculum. These can be utilized as guidelines to provide effective mathematics teachers’ professional development as well as to promote the importance of student-centered instruction.

Diagnostic assessment is a key element in the process of learning mathematics because it can signify what the teachers want their students to know and be able to do and can help teachers to create learning environments that support the attainment of learning standards as indicated in the national mathematics curriculum. Using this line of reasoning, the results of this research imply that what the teachers choose to assess using digital diagnostic tools will end up being the focus of instruction. The results are corresponding to previous researchers’ results (Faber et al., 2017; Gane et al., 2018; Huang et al., 2014; Ketterlin-Geller & Yovanoff, 2009). Besides, the assigned diagnostic MP assessments in the digital diagnostic tool must be best represented in the forms of knowledge and competency and the kinds of learning that teachers want to emphasize. This is because the current education system is designed to require students to possess a higher level of MP in the complex and multidimensional proficiencies which are needed in the 21st century.

However, results imply that there are still some limitations relating to the unclear scoring criteria especially between the MP levels. This requires future researchers to clarify the descriptions in detail for each skill so that the test questions will be designed to be consistent to the students’ MP level while they are developing an assessment framework. Besides, future researchers have to take into consideration the influence of raters in terms of their consistency in assessing the students’ diagnostic tests before analyzing the data. Multidimensional Item Response Theory (MIRT) that used in this research needs to span the range of item difficulties for accurate estimation of the item parameters. Therefore, researchers would like to suggest to future researchers to use a nonrandom sample so that the estimated parameters could later to cover the whole range of different MP levels from the lowest level (logit ≤ -3) to the highest level (logit ≥ +3) (Baker & Kim, 2017; DeMars, 2010).

Although the digital technology can be accessed freely as web-based resources and compatibility with multiple sequences and approaches, the results revealed that the process system component still has problems estimating students’ MP because of the complexity of the algorithm which is a psychometric model. Besides, Adam et al.’s (1997) MRCMLM model were used in this process system component that allowing for the specification of a large number of multidimensional item response models (Draney & Wilson, 2010) because MRCMLM is a general and flexible model. As a result, this model uses design matrices to specify the relationship between responses to the items and structural parameters for a given measurement situation.

In addition, the diagnostic report component of digital technology is beneficial for teachers and students because it allows teachers to post assignments for students and dedicates an online brainstorming session for students at the same time. This has been supported by the experts in their evaluation of digital technology’s suitability aspect. On top of that, it is a real-time tool in assisting teachers to view their students’ feedback on the assessment items (Hwang & Chang, 2011). However, digital technology cannot allow teachers to interact with their peers to provide feedback on the tasks at hand. Consequently, researchers needed to develop multiple ways to provide feedback and apply a formative strategy to create web-based learning as a future step to overcome the current shortcoming. This type of web-based formative assessment has been recognized as an effective approach to assist students to identify learning flaws and thus trigger their motivation for active learning. This enables students to understand the learning content effectively. This argument is supported by past researchers such as
Confrey and Maloney (2015), Cowie and Sakui (2015), Ketterlin-Geller and Yovanoff (2009), and Faber et al. (2017).

Researchers would like to suggest to the Ministry of Education to conduct training for mathematics teachers so that they can utilize the progress maps to measure and the digital technology to diagnose their students’ learning problems. Ultimately, the progress maps of the digital technology will assist them to diagnose their students’ multidimensional MP and improve their MP level as well.

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