# Gompertz and Logistic Models to the Productive Traits of Sunn Hemp

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# Abstract

Studies on growth models for productive character of sunn hemp are important to know the behavior of the culture. Therefore, the objective of this research was to adjust non-linear models, Gompertz and Logistic, in the description of productive traits of sunn hemp in two sowing periods. Two uniformity trials were performed. The evaluations began on October the  $29^{th}$  2014 and December the  $16^{th}$  2014, totaling 94 and 76 evaluation days for periods 1 and 2, respectively. After the emergence of the seeds of sunn hemp, for first period from 7 days after sowing, and from 2 to 13 days after sowing, on each day, they were collected randomly four plants. The traits: fresh matter leaf, stem, root, shoot, and total, and dry matter leaf, stem, root, shoot, and total. For both models the confidence interval was calculated of parameters *a*, *b* and *c*. The adjustment quality of the Gompertz and Logistic models was verified by the determination coefficient, the Akaike information criteria, residual standard deviation, mean absolute deviation, mean absolute percentage error and mean prediction error. The Gompertz model when compared between the sowing periods through the confidence interval of the parameters, for the productive traits, differs. The same result was found for the Logistic model. The growth models of Gompertz and Logistic presented good adjustment quality.

Keywords: Crotalaria juncea, dry matter, fresh matter, nonlinear models

# 1. Introduction

The sunn hemp (*Crotalaria juncea* L.) is a fast-growing species, used as rotating green manure with various crops. According to Wutke, Calegari, and Wildner (2014), sunn hemp has potential for cultivation in both the southeast and Center-West regions as well as in the south region of Brazil as "soil improver" and "recuperate", besides being tolerant to soils of medium fertility. This species stands out among legumes, producing a high amount of dry matter mass per area (Sousa, 2011).

One way to characterize the growth of gives culture is by modeling (Streck, Bosco, Lucas, & Lago, 2008). According to Gomes, Robaina, Peiter, Soares, and Parizi (2014), the crops growth simulation models are important tools to determine the best sowing date, to forecast crops in different scenarios. Currently, several researchers are studying the relationship between two variables, the behavior of a dependent variable as a function of another independent variable(s). The relation can be described by means of mathematical functions, these being denominated regression models.

The analysis of growth curves, involving the adjustment of non-linear regression models, is used to estimate the causes of growth and to infer about the contributions of the various processes present in plant development. According to Fernandes, Pereira, Muniz, and Savian (2014), the study of growth curves, through non-linear models, synthesizes information from a set of date. Among the several models that are used for this purpose, the Gompertz and Logistic models stand out, which contribute or facilitate the interpretation of the processes involved in plant growth, sincerity parameters allow efficient practical interpretations.

The adjustment of non-linear models has been studied in several areas of in the comparison of different non-linear models in banana (Maia, Siqueira, Silva, Peternelli, & Salomão, 2009), Logistic model in describing the growth of fruit dwarf coconut (Prado, Savian, & Muniz, 2013); in the study of models for the estimation of productivity for the soybean crop (Gomes et al., 2014); do not adjust Logistic model of the maize height date (Mangueira, Savian, Muniz, Sermarini, & Crosariol Neto, 2016) and the study of the Gompertz and Logistic

models in the description of cocoa fruit growth (Muniz, Nascimento, & Fernandes, 2017). Therefore, studies on growth models for productive character of sunn hemp are important to know the behavior of the culture, but no work has been found in the literature. It is assumed that these models can adequately describe the productive characteristics of green and dry matter mass of leaf, stem, root, shoot and total of sunn hemp.

The objective of this research was to adjust the non-linear models, Gompertz and Logistic, in the description of the productive character of sunn hemp (*Crotalaria juncea* L.) at two sowing date.

### 2. Material and Methods

Two uniformity trials (experiments without treatments) were conducted with sunn hemp (*Crotalaria juncea* L.) during the 2014/2015 harvest, in an experimental area of the Department of Plant Science at the Federal University of Santa Maria, Rio Grande do Sul State. The sunn hemp seeds were sown on two periods, the first sowing period on October 22, 2014 and the second period on December 3, 2014. On both periods, was performed in rows 0.5 m apart with a density of 20 plants per row meter in a usable area of 52 m  $\times$  50 m (2.600 m<sup>2</sup>).

After the emergence of the seeds of sunn hemp, for first period from 7 days after sowing (October 29, 2014), and from 2 to 13 days after sowing (December 16, 2014), on each day, they were collected randomly four plants, totaled 94 and 76 evaluation days, respectively. The traits were evaluated fresh matter leaf (FML), fresh matter stem(FMS) fresh matter root (FMR), fresh matter shoot (FMSH = FML + FMS), the total fresh matter (FMT = FML + FMS + FMR), dry matter leaf (DML), dry matter stem (DMS), dry matter root (DMR), dry matter shoot (DMSH = DML + DMS), and total dry matter (DMT = DML + DMS + DMR). The leaf fresh matter leaf, stem and root in g were obtained by digital weighing, and the material was oven dried at 60 °C with forced ventilation until constant weight was reached to obtain the dry matter leaf, stem and root.

For these productive traits, the Gompertz and Logistic models were fitted as a function of days after sowing (DAS).

The Gompertz model was given by the equation:

$$yi = a \cdot e^{(-e^{(b-c \cdot xi)})}$$
(1)

and, the Logistic model was given by the equation:

$$yi = \frac{a}{1 + e^{(-b - c \cdot xi)}}$$
 (2)

where, yi is the it observation of the dependent variable, with i = 1, 2, ..., n and n is number the observation; xi is the ith observation of the independent variable; a is the asymptotic value; b is a location parameter without direct practical interpretation but with importance for maintaining the sigmoidal shape of the model; c is associated with growth and indicates the rate of maturity or precociousness. The higher the value of c, the less time is required for the plant to reach the asymptotic value (a).

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The Gompertz model, the inflection point (IP) was calculated by:

$$ci = \frac{b}{c} \tag{3}$$

and,

$$yi = \frac{a}{e} \tag{4}$$

maximum acceleration point (map):

$$xi = \left(\frac{b - \ln(2.6180)}{c}\right) \tag{5}$$

and,

$$yi = a \cdot e^{(-2.6180)}$$
 (6)

maximum deceleration point (mdp):

$$xi = \left(\frac{b - \ln\left(0.3819\right)}{c}\right) \tag{7}$$

and,

$$yi = a \cdot e^{(-0.3819)}$$
 (8)

asymptotic deceleration point (adp):

$$xi = \left(\frac{b - \ln\left(0.1657\right)}{c}\right) \tag{9}$$

and,

$$yi = a \cdot e^{(-0.1657)} \tag{10}$$

where, a, b, and c are model parameters, and e is the base of the neperiano logarithm (Mischan & Pinho, 2014). Also, the Logistic model, the inflection point (IP) was calculated by:

$$xi = \frac{-b}{c} \tag{11}$$

and,

$$yi = \frac{a}{2} \tag{12}$$

maximum acceleration point (map):

$$xi = \left(\frac{-b}{c}\right) - \left(\left(\frac{1}{c}\right) \times 1.3170\right)$$
(13)

and,

$$yi = \frac{a}{4.7321}$$
 (14)

maximum deceleration point (mdp):

$$xi = \left(\frac{-b}{c}\right) + \left(\left(\frac{1}{c}\right) \times 1.3170\right)$$
(15)

and,

$$yi = \frac{a}{1.2679}$$
 (16)

and, asymptotic deceleration point (adp):

$$xi = \left(\frac{-b}{c}\right) + \left(\left(\frac{1}{c}\right) \times 2.2924\right) \tag{17}$$

and,

$$yi = \frac{a}{1.1010}$$
 (18)

where, a, b, and c are model parameters, and e is the base of the neperiano logarithm (Mischan & Pinho, 2014).

Subsequently, the comparison between the growth models adjusted for the traits evaluated, adopted the criterion of overlapping the confidence intervals of the parameters estimated for each model. For this, a growth curve was adjusted for each traits, obtaining the limits of the confidence intervals at  $100 \times (1 - \alpha)$  for the parameters. The comparison will be made by checking whether or not the respective intervals coincide. For example, to compare the epochs for the same traits, when at least one parameter estimate of a traits for a given period contained in the confidence interval of the same traits parameter of another period, they do not differ. However, if none of the estimates are contained in the confidence interval of the other, the parameter estimates differ between them. Statistical software R (R Development Core Team, 2017) was used for this analysis.

The following parameters were utilized to evaluate the goodness of fit of the Gompertz and Logistic models: coefficient of determination:

$$R^2 = SQR/SQT \tag{19}$$

where, SQR is the sum of residue square, SQT is the sum of total square, the best model had the highest  $R^2$  value; Akaike information criterion:

$$AIC = \ln (\sigma^2) + 2(p+1)/n$$
(20)

where,  $\ln(\sigma^2)$  is the logarithm of the variance model, p is parameter of model, and n is number of parameters model, the best model had the lowest value; standard deviation of the residuals:

$$SDR = \sqrt{MSE}$$
 (21)

where, *MSE* is the mean square error, the lower the *QMR* value, the better the fit of the model; mean absolute deviation:

$$MAD = \frac{\sum_{i=1}^{n} |y_i - \hat{y}_i|}{n}$$
(22)

the lower the value, the better the fit of the model; mean absolute percentage error:

$$MAPE = \frac{\sum_{i=1}^{n} \frac{|y_i - \hat{y}_i|}{|y_i|}}{n} \times 100$$
(23)

the best fitting model had the lowest value; and mean prediction error:

$$MPE = \frac{1}{n} \sum_{i=1}^{n} EPi$$
<sup>(23)</sup>

measures the adherence of the estimated data to the obtained data (Maia et al., 2009). The calculations were performed with the help of Microsoft Office Excel® application and software statistic R (R Development Core Team, 2017).

## 3. Results and Discussion

After the Gompertz and Logistic models were established, their suitability was investigated based on the residues. But for the traits FML, FMR, and DMR at the first period, and the traits FML and DML in second period, were transformed through Box-Cox transformation to which these assumptions were met.

By means of the Shapiro-Wilk test, the assumption of residual normality was met in both models for both sowing periods, since this test had a p-value greater than 0.05 for all traits studied. For the test Breusch- Pagan, also based on p-value, it can be inferred that the residual variances were homogeneous in all the traits of the two sowing periods (p > 0.05). Through the Durbin-Watson test, with significance level of 5%, it was found that the residues attended the inde pendence assumption (p < 0.05) for all traits in two sowing periods (Table 1).

Table 1	. Value-p	of the	Shapiro-	-Wilk	(SW),	Breusch-Pa	gan (BP)	and	Durbin	-Watson	(DW)	tests	applied	on
Gomper	tz and Lo	gistic n	nodel resi	idues f	for the	productive t	raits of su	ınn he	emp in t	wo sowii	ng peri	ods		

<b>m</b> :			First sowing pe	eriod	Second sowing period						
Traits	Model		(October 22, 2	014)	(	(December 5, 2014)					
		SW	BP	DW	SW	BP	DW				
FML	Gompertz	0.0500	0.1007	0.0576	0.0817	0.0500	0.0817				
	Logístico	0.0769	0.1510	0.0542	0.0527	0.0501	0.0616				
FMS	Gompertz	0.0576	0.0658	0.9793	0.2983	0.2706	0.1124				
	Logístico	0.1684	0.0500	0.9463	0.0648	0.4048	0.1357				
FMR	Gompertz	0.0963	0.3960	0.5389	0.0619	0.0654	0.7159				
	Logístico	0.1065	0.5155	0.5005	0.1134	0.0760	0.7496				
FMSH	Gompertz	0.0589	0.1651	0.7700	0.1745	0.0900	0.1345				
	Logístico	0.1807	0.1393	0.5958	0.0508	0.1503	0.1236				
FMT	Gompertz	0.0501	0.1088	0.8198	0.2317	0.1213	0.1969				
	Logístico	0.0745	0.0966	0.6693	0.0548	0.1901	0.1879				
DML	Gompertz	0.0879	0.1738	0.3103	0.2449	0.0500	0.2583				
	Logístico	0.1292	0.1726	0.2321	0.2290	0.0502	0.3173				
DMS	Gompertz	0.8002	0.8067	0.9881	0.4266	0.3728	0.9039				
	Logístico	0.8131	0.0500	0.9874	0.3348	0.3589	0.9124				
DMR	Gompertz	0.2777	0.7099	0.1628	0.1790	0.1569	0.6076				
	Logístico	0.1042	0.4578	0.5698	0.1602	0.1893	0.6385				
DMSH	Gompertz	0.4391	0.2132	0.9284	0.3873	0.2884	0.8790				
	Logístico	0.0694	0.5642	0.9184	0.0773	0.2421	0.8545				
DMT	Gompertz	0.2322	0.3253	0.7270	0.4455	0.2395	0.7089				
	Logístico	0.1481	0.3070	0.9298	0.0544	0.1288	0.6085				

*Note.* <sup>\*</sup>FML = fresh matter leaf; FMS = fresh matter stem; FMR = fresh matter root; FMSH = fresh matter shoot and FMT = total fresh matter; DML = dry matter leaf; DMS = dry matter stem; DMR = dry matter root; DMSH = dry matter shoot and DMT = total dry matter.

Therefore, the Gompertz and Logistic models are suitable for adjusting the productive traits of sunn hemp. In study on nonlinear models for description of cacao fruit growth with assumption violations, Muniz et al. (2017), verified the importance of performing the residual analysis.

For the comparison of the model parameters estimates between sowing periods, the criterion of overlapping the confidence intervals of the parameters estimates for each model was used. It is observed that for the Gompertz model to FML, the estimate of the parameter a in first period was 49.32. This estimate was higher than the LI

and less than the LS 95% of the estimate parameter a in second period, that is, is with in 95% of the estimate of the parameter a at the second period. The estimate of the parameter a at the second period was 49.36. This estimate was higher than the LI and less than the LS 95% of the parameter estimates a in the first period, or is with in 95% of the parameter estimates a in the first period. Therefore, the estimates of the parameter a of the periods do not differ to a 5% probability (non-significant effect). However, for the parameters b and c it is observed that there was a significant difference (Table 2).

Table 2. Estimates of the parameters, and respective standard errors (EP) and lower (LI) and upper (LS) limits of the 95% confidence interval, in the fit of the productive traits of fresch matter mass of sunn hemp in two sowing periods

Traits	Parameters		First sowi (October 2	ng period 22, 2014)		Second sowing period (December 3, 2014)					
		Estimation	EP	LI	LS	Estimation	EP	LI	LS		
Model of Gompertz											
FML	a(ns)	49.32	2.5513	44.16	57.66	49.36	12.514	34.44	148.63		
	b (*)	3.38	0.5402	2.3742	5.2469	2.18	0.3814	1.6803	3.3017		
	c (*)	0.0712	0.0118	0.0472	0.1128	0.0373	0.0111	0.0166	0.0660		
FMS	a (*)	128.89	11.70	110.79	162.97	201.92	190.51	190.22	231.12		
	b (ns)	2.90	0.4042	2.2590	3.7939	2.37	0.4001	2.1213	3.8777		
	c (*)	0.0498	0.0085	0.0351	0.0682	0.0309	0.0098	0.0270	0.0401		
FMR	a (*)	31.11	2.8585	26.88	39.13	41.32	2.4500	36.97	47.652		
	b (*)	3.24	0.5120	2.4246	4.3775	2.02	0.3550	1.8701	2.4532		
	c (*)	0.0550	0.0102	0.0377	0.0768	0.0226	0.0088	0.0189	0.0304		
FMSH	a (*)	179.18	14.000	156.06	220.70	274.09	18.700	245.67	296.12		
	b (*)	2.86	0.3942	2.2119	3.7776	2.21	0.3221	1.9804	2.4301		
	c (*)	0.0521	0.0085	0.0367	0.0718	0.0292	0.0093	0.0268	0.0312		
FMT	a (*)	211.43	16.820	184.13	260.36	315.41	21.901	298.76	330.32		
	b (*)	2.87	0.3940	2.2348	3.7760	2.18	0.3150	1.9700	2.2908		
	c (*)	0.0517	0.0084	0.0367	0.0708	0.0283	0.0096	0.0275	0.0309		
Model Logist	ic										
FML	a (*)	46.56	1.7895	42.227	52.352	39.16	5.2881	37.15	45.677		
	<i>b</i> (ns)	-5.95	0.8184	-9.855	-4.412	-4.58	0.6098	-8.500	-3.512		
	c (*)	0.1146	0.0167	0.0796	0.2009	0.0752	0.0143	0.0123	0.1091		
FMS	a (*)	115.80	6.5474	104.19	132.86	201.92	190.49	190.00	230.10		
	b (ns)	-5.53	0.5888	-6.777	-4.623	-5.28	0.3609	-6.600	-4.550		
	c (ns)	0.0871	0.0109	0.0687	0.1107	0.0613	0.0108	0.0105	0.0915		
FMR	a (*)	28.05	1.5719	25.38	31.88	39.22	2.4428	36.90	47.81		
	b (*)	-6.22	0.7633	-7.887	-5.025	-4.87	0.2890	-5.3501	-3.780		
	c (*)	0.0976	0.0136	0.0753	0.1269	0.0505	0.0100	0.0350	0.0701		
FMSH	a (*)	164.36	8.4972	148.42	187.33	238.68	19.914	210.12	270.31		
	b (ns)	-5.28	0.5650	-6.521	-4.390	-4.87	0.2476	-5.3200	-3.550		
	c (ns)	0.0871	0.0108	0.0683	0.1122	0.0599	0.0095	0.0101	0.0910		
FMT	a (*)	193.13	10.016	174.71	219.52	281.63	125.87	260.12	300.01		
	<i>b</i> (ns)	-5.36	0.5679	-6.582	-4.466	-4.85	0.3149	-6.400	-4.531		
	c (*)	0.0875	0.0108	0.0692	0.1112	0.0582	0.0112	0.0368	0.0710		

*Note.* <sup>\*\*</sup>FML = fresh matter leaf; FMS = fresh matter stem; FMR = fresh matter root; FMSH = fresh matter shoot and FMT = total fresh matter.

To estimate the parameter *a* significant effect for the traits FML, FMS, FMSH and FMT; to *b* significant effect parameter to the traits FMS, FMSH and FMT; and *c* significant effect parameter to the traits FML, FMS, FMR,

FMSH and FMT (Table 2). So for the Gompertz model, the parameter estimates a, b and c differ a 5% probability between the sowing periods.

Reading the Logistic model, it is observed that for the parameter a significant effect on the traits FML, FMS, FMR, FMSH and FMT; for the parameter b, a significant effect only for the character MVR; and the c significant effect parameter to the traits FML, FMR and FMT. So for the Logistic model, the parameter estimates a, b and c differ a 5% probability between sowing periods (Table 2). These results are important as it is observed that sowing periods have influence on the production of fresh matter mass in sunn hemp, and for productive purposes second period provided higher values of fresh matter mass. In study on to fit Gompertz and Logistic nonlinear to descriptions of morphological traits of sunn hemp, Bem, Cargnelutti Filho, Facco, Schabarum, Silveira, Simões, and Uliana (2017), also used for the comparison of the model parameters estimates between sowing periods, the criterion of overlapping the confidence intervals, highlighting the importance of this methodology.

In relation to the mass of dry matter, it is observed for the Gompertz model for DML, DMS, DMSH and DMT, significant effect on the parameter a, to the parameter b, a significant effect only for the character DML, and parameter c, a significant effect on the traits DML and DMSH (Table 3). Therefore, it is concluded that the estimates of the parameters a and b of periods differ at 5% probability. For Logistic model, it is observed that for the parameter, there was a significant effect for all productive traits for the parameter b and c, a significant effect on the character DMR (Table 3).

Traits	Parameters		First sowin (October 22	g period 2, 2014)		Second sowing period (December 3, 2014)					
		Estimation	EP	LI	LS	Estimation	EP	LI	LS		
Model of C	Gompertz										
DML	<i>a</i> (ns)	11.56	0.9300	10.09	14.24	26.74	1.6300	23.15	31.00		
	b (*)	2.89	0.4400	2.1809	3.8914	2.09	0.6640	1.9402	2.4304		
	c (*)	0.0536	0.0094	0.0371	0.0748	0.0238	0.0110	0.0101	0.0302		
DMS	a (*)	33.19	3.4212	28.28	42.96	95.64	7.8100	90.05	100.30		
	b (ns)	3.51	0.5236	2.6575	4.7132	3.58	58 0.5500		4.8004		
	c (*)	0.0542	0.0097	0.0375	0.0754	0.0415	0.0088	0.0355	0.0690		
DMR	a (*)	9.76	1.1280	8.24	13.09	12.99	0.7445	10.40	17.03		
	b (*)	3.67	0.6672	2.1115	5.2218	2.27	0.6680	2.1680	5.2311		
	c (*)	0.0575	0.0123	0.0369	0.0841	0.0252	0.0011	0.0192	0.0303		
DMSH	a (*)	46.17	4.7840	39.33	59.63	115.28	9.7093	110.00	125.90		
	b (*)	3.11	0.4415	2.4055	4.0816	3.03	0.4402	2.4321	4.1012		
	c (*)	0.0497	0.0087	0.0347	0.0680	0.0354	0.0900	0.0270	0.0412		
DMT	a (*)	56.07	5.7535	47.88	72.09	127.11	10.050	112.12	134.06		
	b (*)	3.18	0.4557	2.4570	4.1894	2.98	0.4776	2.5031	4.2345		
	c (*)	0.0507	0.0089	0.0348	0.0693	0.0342	0.0909	0.0268	0.0421		
Model Log	gistic										
DML	a (*)	10.66	0.5727	9.65	12.12	26.74	1.6213	23.12	30.14		
	b (ns)	-5.34	0.6306	-6.690	-4.351	-5.13	0.6210	-6.300	-4.300		
	c (*)	0.0895	0.0123	0.0691	0.1163	0.0536	0.0120	0.0750	0.1100		
DMS	a (*)	28.86	1.6542	26.07	32.96	95.64	7.8120	90.12	100.79		
	b (ns)	-7.00	0.7893	-8.789	-5.731	-8.74	0.0905	-9.001	-7.600		
	<i>c</i> (ns)	0.1021	0.0131	0.0800	0.1314	0.0966	0.0113	0.0800	0.1210		
DMR	a (*)	8.64	0.5682	7.74	10.01	12.99	0.7444	10.23	16.00		
	b (*)	-7.26	1.0076	-9.515	-5.675	-5.67	0.6300	-6.3800	-4.200		
	c (*)	0.1066	0.0166	0.0798	0.1428	0.0589	0.0810	0.0510	0.0700		
DMSH	a (*)	40.15	2.3365	36.36	45.85	115.28	9.7090	100.01	123.00		
	b (ns)	-6.23	0.6683	-7.671	-5.165	-7.29	0.7788	-8.600	-5.500		
	<i>c</i> (ns)	0.0932	0.0117	0.0737	0.1179	0.0801	0.0105	0.0721	0.0914		
DMT	a (*)	48.84	2.8107	44.19	55.60	127.11	10.000	110.31	134.15		
	b (ns)	-6.38	0.6899	-7.868	-5.280	-7.38	0.7798	-8.5001	-5.9552		
	c (*)	0.0951	0.0119	0.0752	0.1203	0.0813	0.0102	0.0720	0.0920		

Table 3. Estimates of the parameters, and respective standard errors (EP) and lower (LI) and upper (LS) limits of
the 95% confidence interval, in the fit of the productive traits of dry matter mass of sunn hemp in two sowing
periods

*Note.* <sup>\*</sup>DML = dry matter leaf; DMS = dry matter stem; DMR = dry matter root; DMSH = dry matter shoot and DMT = total dry matter.

Therefore, it is concluded that for the Logistic model, the parameter estimates a, b and c of periods differ at 5% probability. This, as for the traits of mass of fresch matter, also, it is concluded that the sowing periods have influence on the mass production of dry matter.

Thes setting quality criteria of the Gompertz and Logistic models are very important to compare which is the best model. It is observed that for the traits of FML, FMS, FMR, FMSH and FMT for the first period, the values for criteria R, AIC, DPR, DMA and MAPE were similar for both models, indicating that in order overall, there was a good adjustment of the models. For the EPM evaluation criteria, the values differed between the adjusted models and between the sowing periods for both the fresch matter mass and the dry matter mass of the traits (Table 4).

However, for second period, the quality of fit of the models was lower in relation to the characteristics of first period. It can be inferred that in second period, when sowing of the sunn hemp was later, flowering occurred at 88 DAS, that is, it had a lower cycle when compared to first period, when flowering occurred at 100 DAS, and this may have contributed to the quality of fit of the models. Similar results were observed for the traits DML, DMS, DMR, DMSH and DMT (Table 4).

Table 4. Criteria for evaluation the quality fit: coefficient of determination ( $R^2$ ), Akaike information criterion (AIC), standard deviation of residuals (SDR), mean absolute deviation (MAD), mean absolute percentage error (MAPE), and mean prediction error (MPE) for Gompertz and Logistic models, for traits productive of mass of fresch matter, using days after sowing during two sowing periods

Traits		First sowing period (October 22, 2014)							Second sowing period (December 03, 2014)					
Traits	$R^2$	AIC	DPR	DMA	MAPE	EPM	$R^2$	AIC	DPR	DMA	MAPE	EPM		
Model of (	Gompert	Ζ												
FML	0.61	5.48	29.31	0.0006	0.0024	-0.2354	0.49	4.98	20.92	0.0008	0.0057	-0.5038		
FMS	0.67	6.77	55.74	0.0034	0.0075	-0.7465	0.59	6.57	48.12	0.0005	0.0016	0.1403		
FMR	0.63	4.17	15.16	0.0000	0.0004	0.0358	0.41	3.36	9.70	0.0000	0.0052	-0.4552		
FMSH	0.67	7.54	81.78	0.0047	0.0069	-0.6901	0.57	7.28	68.78	0.0019	0.0041	-0.3645		
FMT	0.69	7.83	95.59	0.0049	0.0062	-0.6226	0.56	7.51	77.25	0.0016	0.0031	-0.2704		
DML	0.62	2.28	5.92	0.0001	0.0018	-0.1792	0.45	2.42	6.06	0.0000	0.0011	0.0925		
DMS	0.69	3.91	13.37	0.0002	0.0000	0.2025	0.54	4.58	17.88	0.0087	0.1030	9.0606		
DMR	0.60	1.93	4.95	0.0002	0.0065	0.6539	0.42	0.98	2.95	0.0001	0.0045	0.3674		
DMSH	0.69	4.57	18.54	0.0001	0.0005	0.0504	0.53	5.13	23.46	0.0082	0.0696	6.1264		
DMT	0.67	4.96	22.56	0.0003	0.0015	0.1468	0.53	5.32	25.88	0.0082	0.0628	5.5258		
Model Log	gistic													
FML	0.60	5.50	29.61	0.0041	0.0174	-1.7385	0.49	4.99	21.86	0.0029	0.0198	-1.7393		
FMS	0.67	6.78	56.20	0.0102	0.0228	-2.2753	0.60	6.56	48.10	0.0083	0.0256	-2.2600		
FMR	0.63	4.17	15.18	0.0014	0.0128	-1.2782	0.41	3.36	9.69	0.0008	0.0153	-1.3448		
FMSH	0.66	7.56	82.64	0.0158	0.0230	-2.3043	0.57	7.28	69.00	0.0122	0.0260	-2.2898		
FMT	0.67	7.84	95.50	0.0175	0.0220	-2.2002	0.56	7.52	77.46	0.0122	0.0236	-2.0738		
DML	0.62	2.29	5.95	0.0009	0.0169	-1.6904	0.46	2.42	6.04	0.0004	0.0131	-0.0131		
DMS	0.69	3.91	13.37	0.0011	0.0114	-1.1383	0.57	4.52	17.32	0.0075	0.0884	7.7768		
DMR	0.60	1.92	4.94	0.0002	0.0051	-0.5108	0.42	0.98	2.94	0.0001	0.0079	-0.6915		
DMSH	0.69	4.57	18.56	0.0018	0.0127	-1.2680	0.55	5.08	22.87	0.0054	0.0459	4.0380		
DMT	0.68	4.96	22.57	0.0020	0.0115	-1.1456	0.55	5.28	25.29	0.0092	0.0698	6.1386		

*Note.* <sup>\*</sup>FML = fresh matter leaf; FMS = fresh matter stem; FMR = fresh matter root; FMSH = fresh matter shoot and FMT = total fresh matter; DML = dry matter leaf; DMS = dry matter stem; DMR = dry matter root; DMSH = dry matter shoot and DMT = total dry matter.

According to Moura , Souza, Silva, Soares, Carmo, and Brandão (2011), a study on the growth Expolinear models, Logistic and Gompertz on the dry matter accumulation of cultures feijão-cowpea and maize found values of the coefficient of determination higher than 0.97 for all models using as a variable independent DAS; Prado et al. (2013) studied the growth of fruit dwarf coconut, compared Logistic and Gompertz model, according to the following set of criteria: the adjusted coefficient of determination ( $R^2aj$ ), the residual standard deviation (RSD) and Akaike information criterion (AIC), Reis, Cecon, Puiatti, and Finger (2014) comparing five non-linear regression models to describe the accumulation of different dry mass of garlic over time and Lúcio, Sari, Rodrigues, Bevilaqua, Voss, Copetti, and Faé (2016), a study on nonlinear models for estimating cherry tomato yield. Thus, these works are in line with the research objective, adjusting the Gompertz and Logistic models for the productive traits of sunn hemp.

In Figures 1, 2, 3 and 4 are presented mented the growth curves and the corresponding equation and is the inflection point (IP) the models of Gompertz and Logistic in the two sowing periods.



Figure 1. Adjusted to fit Gompertz and Logistic, and IP (inflection point), for the productive traits, fresh matter leaf (FML); fresh matter stem (FMS); fresh matter root (FMR); fresh matter shoot (FMSH) and total fresh matter (FMT), of sunn hemp in first sowing period (October 22, 2014)



Figure 2. Adjusted to fit Gompertz and Logistic, and IP (inflection point), for the productive traits dry matter leaf (DML); dry matter stem (DMS); dry matter root (DMR); dry matter shoot (DMSH) and total dry matter (DMT), of sunn hemp in first sowing period (October 22, 2014)

*Note.* \*First sowing periods = October 22, 2014 and evaluation = October 29, 2014 (xi = 7). \*\*Left column Gompertz model and right column Logistic model.  $\blacksquare$  maximum acceleration points (map);  $\bullet$  Inflection points;  $\blacktriangle$  maximum deceleration points (mdp) and  $\bigstar$  asymptotic deceleration points (adp) (xi; yi).



Figure 3. Adjusted to fit Gompertz and Logistic, and IP (inflection point), for the productive traits, fresh matter leaf (FML); fresh matter stem (FMS); fresh matter root (FMR); fresh matter shoot (FMSH) and total fresh matter (FMT), of sunn hemp in second sowing period (December 3, 2014)

*Note.* \*Second sowing periods = December 3, 2014 and evaluation = December 16, 2014 (xi = 13). \*\*Left column Gompertz model and right column Logistic model.  $\blacksquare$  maximum acceleration points (map); • Inflection points;  $\blacktriangle$  maximum deceleration points (mdp) and  $\bigstar$  asymptotic deceleration points (adp) (xi; yi).



Figure 4. Adjusted to fit Gompertz and Logistic, and IP (inflection point), for the productive traits dry matter leaf (DML); dry matter stem (DMS); dry matter root (DMR); dry matter shoot (DMSH) and total dry matter (DMT), of sunn hemp in second sowing period (December 3, 2014)

*Note.* \*Second sowing periods = December 3, 2014 and evaluation = December 16, 2014 (xi = 13). \*\*Left column Gompertz model and rigth column Logistic model.  $\blacksquare$  maximum acceleration points (map);  $\bullet$  Inflection points;  $\blacktriangle$  maximum deceleration points (mdp) and  $\bigstar$  asymptotic deceleration points (adp) (xi; yi).

It is observed that the maximum acceleration point (map) occurs at the beginning of the curve and ends when the culture reaches the IP, at this moment it is possible to infer about the maneuvers to be carried out in the jungle grove such as fertilization, pest and diseases, herbicide application, because the plant will respond to these

managements efficiently. Then, the curve starts to stabilize the growth, at which point the maximum deceleration point (mdp) occurs, stabilizing the growth until reaching the point of asymptotic deceleration (adp), at this stage the crop reaches flowering. Therefore, all these points are important for future projections and for planning activities with culture.

### 4. Conclusions

The Gompertz and Logistic models compared between sowing periods through the parameters of the confidence intervals for the traits fresch matter mass and dry matter mass leaf, stem, root, shoot and total differ.

The Gompertz and Logistic models, adjusted to fresch matter mass and dry matter mass data showed good ft.

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