Calculation of Agricultural Drain Spacing Taking into Account Regularity of Water Exchange in the Vadose Zone

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Abstract

Conventional analytical formulae for calculation of subsurface drain spacing for maintaining a desired water table depth in agricultural areas, such as Hooghoudt's formula, are based on using the ratio between the soil saturated hydraulic conductivity K_s and the groundwater recharge rate q. It is well known that selection of the q value as one of the principle drainage criterion is one of the problems of the drain spacing calculation. In this paper, it is illustrated that for steady state conditions and, in case of homogeneous soil profile, the ratio q/K_s can be substituted by an analytical function that takes into account the regularity of infiltration through the vadose zone. This function can be derived from the soil moisture content in the root zone and other well-known hydrodynamic soil parameters. An example of drain spacing calculation is presented.

Keywords: agricultural drainage, design, soil water regime

1. Introduction

In practice, subsurface drainage design for maintaining the depth of the water table at a particular depth is performed by using equations based on steady state water flow in saturated and unsaturated zones of soil profile. For calculation of the horizontal drain spacing, it is necessary to know the value of the groundwater recharge rate q and the soil's saturated hydraulic conductivity K_s . Additionally, information about climatic and hydrogeological conditions as well as the type of land use (rain-fed or irrigation, and subsurface drainage together with surface drainage or without it among others) are necessary to complete the calculation. The q value is one of the main drainage criteria and it frequently ranges between 1 to 10 mm/day. To date, there are no well-defined criteria concerning the q values; however, it depends on various factors that should be taken into consideration, *i.e.*, waterlogging, climatic, soil and hydrogeological conditions and the type of land use. As regards the former, Ritzema (1994) proposed some criteria for the selection or assessment of q values. The general form of the equation used to calculate the drain spacing L (m) in homogeneous soils can be expressed for steady state conditions by (Ritzema, 1994; Skaggs and van Schilfgaarde, 1999; Mishra and Singh, 2007; Hay, 2010; Averyanov, 2015):

$$L = f_1[(K_s/q) \times f_2(h, r_{dr}, \Phi)]$$
(1)

Where, f_1 and f_2 correspond to analytical functions; K_s is the saturated hydraulic conductivity (m/day); q is the groundwater recharge rate or drain discharge rate (note that K_s and q have the same dimension - m/day); h is a water table height in the middle of drain-spacing above the water level in drains (m): $h = d_{dr} - d_{wt}$; d_{dr} is drain depth (m), d_{wt} is the depth to the water table (m), r_{dr} and Φ are the drain radius and "hydraulic resistance", respectively (m). A specific case of the relationship (1) is Hooghoudt's formula (Ritzema, 1994):

$$L = 2h\sqrt{\frac{K_s}{q}\left(1 + \frac{2D_e}{h}\right)} \tag{2}$$

Where, L corresponds to the drain spacing (m); D_e is an "equivalent depth" (m) determined from Hooghoudt's graphs, and D_e represents the "hydraulic resistance", which takes into account the drain radius and the relationship between the depth to the impermeable layer and the drain spacing.

Analytical equations for calculating the drain spacing on agricultural areas do not take into account the soil moisture content in the root zone and the unsaturated hydraulic properties of soils. Moreover, it is commonly assumed that the groundwater recharge rate between drains is uniformly distributed (Ritzema, 1994; Skaggs & van Schilfgaarde, 1999; Christen et al., 2001; Kladivko et al., 2004; Mileham et al., 2008; Fuentes et al, 2009). For steady state conditions, the groundwater recharge rate is equal to the infiltration rate through the vadose zone. Currently, there are well-developed methods for the vadose zone; however, there is a practical need to derive a simple approach for calculating the drainage spacing by means of analytical formulae. These calculations should incorporate the unsaturated hydraulic conductivity and soil water retention functions of the vadose zone. Furthermore, calculations should also consider the soil moisture content in the root zone (Nikolskii, 1998). One way to include the hydrodynamic properties of vadose zone in the determination of drain spacing is by means of computer programs, which can calculate the water movement in the unsaturated and saturated zones of the soil profile.

The purpose of this paper is to develop an analytical formula for calculating the drain spacing by making use of soil moisture content in the root zone, the water table depth, and other well-known hydrodynamic soil parameters.

2. Method

The main assumptions used in developing the method proposed herein are:

> The soil profile is homogenous;

> The moisture content θ_r is maintained in a root zone of thickness z_r , at $z = z_r/2$ during a certain period, *i.e.*, a week, month, growing season or year; and

> The groundwater recharge rate q (m/day) in steady state conditions is equal to the vertical flow rate through the vadose zone determined from Darcy's law for unsaturated soils. This relationship can be expressed as:

$$q = K_{\theta}(\mathrm{d}P_{\theta}/\mathrm{d}z - 1) \tag{3}$$

Where, K_{θ} is the unsaturated hydraulic conductivity (m/day) as a function of the volumetric moisture content θ (m³/m³); P_{θ} is the matrix potential of soil water (m) as a function of the moisture content θ , and z corresponds to the depth from the soil surface (m).

The unsaturated hydraulic conductivity as a function of the volumetric moisture content $K_{\theta}(\theta)$ and the matrix potential of soil water as a function of the moisture content $P_{\theta}(\theta)$ are given by (Averyanov, 1949 & 2015; Brooks & Corey, 1964; van Genuchten, 1980; Mualem, 1978):

$$K_{\theta} = K_{s} f_{3}(\theta) \tag{4}$$

and,

$$P_{\theta} = P_0 f_4(\theta) \tag{5}$$

Where, K_s is the saturated hydraulic conductivity (m/day); P_0 is a constant of the relationship $P_d(\theta)$ (m), and $f_3(\theta)$ and $f_4(\theta)$ are functional relationships for Equations (4) and (5).

To determine the ratio K_s/q , one can integrate Equation (3) by using the following boundary conditions:

 $z = z_r/2$ (z_r is the root zone depth), the moisture content is $\theta = \theta_r$. At this condition the saturation S is defined by the following boundary condition expression:

$$S = S_r = (\theta_r - \theta_0)/(\theta_S - \theta_0)$$
(6)

Where, θ_s is the saturation soil moisture content, and θ_0 is the residual moisture content. At the water table $z = d_{wts}$ the moisture content is given by:

$$\theta = \theta_{\rm S}$$
 and the saturation $S = 1$ (7)

Using the boundary condition given by Equation (6) and by integrating Equation (3), one can obtain:

$$(d_{wt} - \frac{z_r}{2}) = \int_{S_r}^{1} \frac{P_{\theta}'(S)dS}{1 - \frac{q}{K_{\theta}}}$$
(8)

Where, $K_{\theta} = K_{\theta}(S)$. The solution of Equation (8) expressed as a ratio of K_{θ}/q or K_s/q depends on the functions $P_{\theta}(S)$ and $K_{\theta}(S)$. This means that a drain spacing *L* can be calculated by means of Equation (1) or by using Equation (2) without the ratio K_s/q . This can be achieved with the aid of well-known parameters, such as climatic conditions, the hydrodynamic soil properties $P_{\theta}(S)$ and $K_{\theta}(S)$, the soil moisture content in the root zone θ_r (or S_r) and the depth to the water table d_{wr} without having selected the groundwater recharge rate *q* in advance.

3. Results and Discussion

As an example, we consider the water retention function given by Richards (Ritzema, 1994):

$$P_{\theta} = P_0 \ln S \tag{9}$$

Where, $P_0 > 0$ and it corresponds to the air entry pressure depending on soil texture; $S = (\theta - \theta_0)/(\theta_s - \theta_0)$, and the unsaturated hydraulic conductivity function given by (Averyanov, 1949 & 2015; Brooks & Corey, 1964):

$$K_{\theta} = K_s S^n \tag{10}$$

Where, n is an exponent ranging from 3.5 to 24.5 depending on the soil texture and structure (Mualem, 1978). Combining Equations (8) and (9) and (10), it gives as a result:

$$\frac{q}{K_s} = \frac{S_r^n - \exp(-\delta)}{1 - \exp(-\delta)} \quad \text{or} \quad \frac{K_s}{q} = \frac{1 - \exp(-\delta)}{S_r^n - \exp(-\delta)} \tag{11}$$

Where, δ corresponds to the dimensionless depth to the water table calculated from half the depth to the water table and it can be expressed as:

$$\delta = n(d_{wt} - z_r/2)/P_0$$
(12)

According to Equation (11), the condition where the groundwater recharge is greater than zero (q > 0) takes place when $S_r^n > \exp(-\delta)$. In general, the q value increases as θ and d_{wt} increase. For a shallow water table, *i.e.*, when $S_r^n < \exp(-\delta)$, the upward water flow (q < 0) takes place. For a deep groundwater table (approximately when $d_{wt} \ge 2$ m), *i.e.* when $S_r^n >> \exp(-\delta)$, the groundwater recharge q can be expressed as a function of the root zone saturation given by:

$$q = K_s S_r^n \tag{13}$$

Obviously, Equation (11) is valid only for shallow groundwater, *i.e.*, when d_{wt} is small and strongly influences the soil moisture content in the root zone, and θ_r or S_r cannot be considered as an independent variable. For a given shallow water table, if calculated values of upward flow q exceed the potential evapotranspiration ET_0 , it is necessary to take $q = ET_0$. Similar to Equation (8), this approach has been used to calculate the maximum value of steady upward flow from the water table to the root zone by Anat et al. (1965) and Wesseling (1991).

In order to verify if Equation (11) describes objectively the regularity of water exchange in the vadose zone, experimental data published by Pchyolkin (2003) were used. These data were obtained in Russia in two experimental stations: one with peat soil and another with alluvial loamy soil. Each experimental station included 8 cylindrical lysimeters with non-altered soil columns of 2 m depth and a surface of 2 m^2 , in which different water table depths were studied. The water balance in the vadose zone for periods of 3 to 5 days is obtained by the expression:

$$W_f = W_{in} + Pr + Ir - ET \pm q \text{ or } W_f - W_{in} = Pr + Ir - ET \pm q$$
(14)

Where, W_f and W_{in} are the water storage in the soil profile above the water table at the end and the beginning of each period, respectively (mm); Pr is the precipitation (mm), Ir is the irrigation (mm), ET corresponds to the evapotranspiration (mm/day), and q corresponds to the water exchange value between the vadose zone and ground water (mm/day) (+q and -q correspond to upward and downward flow, respectively). The lysimeters with peat soil and with alluvial loamy soil had spring wheat and beat roots respectively and both under sprinkle irrigation. The water table in all experiments was maintained at depths ranging from 0.5 to 2 m. The following considerations were taken for the experiments with spring wheat, when $d_{wt} \ge 1$ m, $z_r = 0.5$ m, and for $d_{wt} = 0.5$ m, $z_r = 0.3$ m. In the case of the experiments with beat roots, when $d_{wt} \ge 1$ m, $z_r = 0.4$ m, and for $d_{wt} = 0.5$ m, $z_r = 0.2$ m.

The hydrodynamic properties of these soils were the following:

Peat soil: $\theta_s = 0.85$, $\theta_0 = 0.45$, $K_s = 0.26$ m/d, $P_0 = 1.08$ m; alluvial loamy soil: $\theta_s = 0.52$, $\theta_0 = 0.25$ (all in volumetric units), $K_s = 0.25$ m/d, $P_0 = 1.08$ m.

The soil moisture content values in the root zone of the studied soils were:

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Peat soil: $0.55 < \theta_r \le 0.80$ or $0.25 < S_r \le 0.87$.

Alluvial loamy soil: $0.35 < \theta_r \le 0.45$ or $0.37 < S_r \le 0.74$.

Figure 1 shows the results calculated from Equation (11) and the measured values of q/K_s ratio for samples of peat soil and alluvial loamy soil. The normalized mean square error of calculated and measured data of q/K_s is less than 10 % when using n = 6.4 for peat soil samples and n = 7 for alluvial loamy soil samples. Thus, the results suggest that experimental data can be accurately described by Equation (11) when n values correspond to 6.4 and 7 for peat and alluvial loamy soil samples, respectively.

In the case of homogeneous soil profile, the ratio K_s/q from Equation (11) could be used for calculating drain spacing *L* from Equation (1) or in particular with Hooghoudt's formula (Equation (2)). Substituting Equation (11) in Equation (2), the modified Hooghoudt's formula can be expressed as:

$$L=2h\sqrt{\left(\frac{1-\exp(-\delta)}{S_r^{\ n}-\exp(-\delta)}\right)\left(1+\frac{2D_e}{h}\right)}$$
(15)



Figure 1. Comparison between q values calculated with Equation (11) (solid lines) and those measured in lysimeters (points) with non-altered columns of a peat soil for spring wheat (a) and an alluvial loamy soil for beat roots (b) with sprinkle irrigation. In Figure 1a, plot 1 corresponds to dimensionless water table depth δ = 2.07 (or dimension depth d_{wt} = 0.5 m); plot 2, δ = 4.44 (1.0 m); plot 3, δ = 7.41 (1.5 m); plot 4, δ = 10.37 (2.0 m); in Figure 1b, plot 1, δ = 4.48 (1.0 m); plot 2, δ = 7.28 (1.5 m)

Equation (15) shows that drain spacing L depends not only on the ratio K_s/q but on the soil water saturation S_r (or soil moisture content θ_r) and the dimensionless water table depth δ (or dimensional depth d_{wt}), as well as on hydrodynamic soil characteristics θ_s and θ_0 , and parameters P_0 and n. Equation (15) can be used in practice to calculate drain spacing L and reveals that L value is very sensitive to the soil moisture content in the root zone. To calculate drain spacing for a certain plot it is not necessary to select unknown recharge rate q from bibliography, but it is necessary to know values of θ_s , θ_0 , P_0 and n for Equation (15). These data, which depend on soil texture, can be obtained from experiments or from publications like the one reported by Fuentes Ruiz, Havercamp and Parlange (1991). It is also possible to make previous calibration of drain spacing calculations for selected plot with Equation (15) comparing these data with local or regional L values from field drainage.

Some scenarios as well as a practical example concerning the proposed approach for drain spacing calculation are given below. Figure 2 depicts one of the scenarios used herein to calculate the drain spacing L for homogeneous soil profile and steady state condition.



Figure 2. A schematic representation to calculate drain spacing *L* for homogeneous soil profile and steady state condition

3.1 Scenarios Concerning Drain Spacing

3.1.1 Case 1. Agricultural Irrigated Non-Saline Land with Homogeneous Soil Profile, sprinkle irrigation and Pipe Distribution of Water

In this case for steady state condition, deep percolation of irrigation water through soil profile is equal to groundwater recharge rate q and the expression $\frac{1-\exp(-\delta)}{S_r^n - \exp(-\delta)}$ in Equation (15) can be calculated depending on the soil moisture content in a root zone θ_r (or saturation S_r) and the water table depth d_{wt} (or its dimensionless value δ).

3.1.2 Case 2. Rainfed Land in Humid Zone

The scenario here is more complicated due to the following considerations:

> On one side, the relationship $\frac{1-\exp(-\delta)}{S_r^*-\exp(-\delta)}$ in Equation (15) can be calculated depending on particular or permissible values of θ_r (or S_r) and d_{wt} (or δ). So, it seems that in this case, the use of saturated hydraulic conductivity K_s is necessary;

> On the other side, the value of q could be obtained from the analysis of water balance at the land surface as the difference between precipitation Pr and evapotranspiration ET and water runoff; and

> The calculation of L should be carried out taking into account the two considerations mentioned above. This means that it is necessary to estimate a particular value of q with Equation (11). To achieve this, particular or permissible values of θ_r (or S_r) and d_{wt} (or δ) can be used; however, the value of K_S should be known in advance.

3.1.3 Case 3. Cold Humid Zones Where Subsurface Drainage Is More Intensive in Spring Time Just after Snow Melting

The main purpose of drainage in this season period is to lower down the water table and reduce soil moisture content in the arable soil layer (θ_{ar}) up to a desirable (and known) level during a limited time. Therefore, the value of q/K_s can be calculated by means of Equation (11) considering soil moisture values of arable layer (with thickness, $z_r = 0.2$ -0.3 m and $\theta_r = (\theta_{ar} + \theta_s)/2$) instead of traditional calculation of q.

3.2 Calculation Example

The irrigated site had of loamy, non-saline, homogeneous soil with a deep impermeable layer (more than 50 m). The hydrodynamic parameters of this soil are the following: $K_s = 0.2 \text{ m/day}$, $\theta_s = 0.50$, $P_0 = 0.8 \text{ m}$, and n = 4.1 for $\theta_0 = 0.12$. Note that the exponent *n* depends on the choice of the residual moisture content θ_0 and that *n* decreases as θ_0 increases. Sprinkle irrigation was used for this study. The average thickness of the root zone z_r corresponds to 0.7 m and the soil moisture content θ_r corresponds to 0.24. According to FAO (1980), in such conditions (relatively low permeable and non-saline soil) the *q* value is recommended to be 0.0015 m/day. The depth of drainage pipes, d_{dr} , is 2 m, the depth from drains to the impermeable layer, d_{il} , is 50 m and the desirable depth to water table, d_{wts} , is considered to be 1.5 m. The diameter of drainage pipes is 0.1 m.

By substituting these values into the Hooghoudt's equation (Equation (2)), it results that the value of h, D_e and L corresponds to 0.5 m, 4.92 m and $38 \approx 40$ m, respectively.

In order to use the proposed method, we should first determine S_r and δ . Thus, S_r is equal to (0.24 - 0.12)/(0.50 - 0.12) = 0.316 and δ is equal to 4.1(1.5 - 0.7/2)/0.8 = 5.89. After substituting these parameters into Equation (11),

one obtain that $q/K_s = (1 - e^{-5.89})/(0.316^{4.1} - e^{-5.89}) = 162$ or using directly Equation (15), it results in a drainage spacing *L* of 45 m.

4. Conclusions

Analytical methods for calculating drain spacing L are based on the values of the groundwater recharge and the saturated hydraulic conductivity of the soil. However, the design of subsurface drainage should take into consideration the value of the moisture content in the root zone, as well as the unsaturated hydraulic properties of soils in the vadose zone. In this paper, it is developed an approximate analytical solution for estimating the ratio K_s/q , which can be used for calculating the drainage spacing as a function of the moisture content in the root zone, the depth to the water table, as well as other parameters such as the water retention function and the unsaturated hydraulic conductivity. The example results showed the feasibility of using a modified Hooghoudt's equation. This approach is also applicable to other equations, which contain the ratio K_s/q , such as Kirkham's and Glover equations (Ritzema, 1994). Unfortunately, the determination of the soil water retention and the unsaturated hydraulic conductivity functions is not easy and may cause some uncertainty of q values. However, the described approach can be used at least to take into account the desirable water table depth and some specific characteristics of climate and soil, such as soil moisture content in the root zone and soil texture, in order to understand the dependence of groundwater recharge rate q on the referred characteristics and finally to justify and select q values for subsurface drainage design.

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