A Case Study of Mesospheric Wave Periods and Horizontal Structures over a Low Latitude Station, Allahabad (India)

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Abstract

We report the measurements of short period gravity waves with the help of all sky imager operated at OH nightglow wavelenghts during 21-22 and 23-24 April 2009 from Allahabad (25.5° N, 81.9° E), India. We note persistent oscillations on both the nights with wave periods ranging from 0.4 to 1.5 hours. To quantify the zonal and meridional scales of these waves, we analyze the intensity variability noted in zenith angles 30° , 15° and 0° in East, West, North and South directions. We find the wavelengths of observed waves to vary from 40 to 100 km. We discuss these observed wave properties in connection to their importance in global circulation of upper atmosphere.

Keywords: airglow, mesosphere, gravity waves

1. Introduction

Gravity waves and tides are the important dynamical drivers of the mesosphere-lower thermosphere (MLT) region. Gravity waves are created by the action of gravity on the density variations in the stratified troposphere from passage of wind over topographic structures, frontal, dust-storm and convective activity, and wind shears and have periods typically ranging between few minutes to 3 hours (e.g., Das et al., 2011; Taori et al., 2012a and references cited therein); whereas, tides are a consequence of heating due to absorption of solar infrared and ultraviolet radiation by the tropospheric water vapour and stratospheric ozone, respectively (Forbes and Wu, 2006 and references cited therein). These waves propagate upwards as well as horizontally with the amplitude growing with height (due to negative density gradient of the atmosphere). At mesospheric altitudes, their amplitudes grow many-folds and they become convectively unstable (thereby attaining the saturation limit). Ultimately they break and dissipate momentum and energy to the background atmosphere (Hines, 1960). As such, these upward propagating gravity wave and tides strongly govern the atmospheric circulation, thermal structure and chemical composition at the MLT heights through the dissipation of energy and momentum (Fritts & Alexander, 2003). An assessment of the effects of these gravity waves in global circulation models is difficult because firstly, they are highly variable (i. e. they may exist on a given night, while may not be present on the other one), and secondly, the observations of their periodicity, horizontal and vertical wavelength is difficult. In particular, the short period gravity waves having periodicity less than 3 h lack sufficient observations owing to the required high time resolution. Of late, the ground-based, satellite-borne and in-situ measurements have addressed enormously to our understanding of gravity waves and their profound influence in the MLT variabilities.

Among other ground-based techniques (viz. VHF/ UHF/ MF/ MU/ Meteor radars, falling spheres and lidar instrumentation), airglow observations have been widely used to study the gravity wave and tidal features at the MLT altitudes (e.g., Taori et al., 2005; Guharay et al., 2008; Taori & Taylor, 2010). On course of their propagation through the airglow emission layer, gravity waves or tides induce variability in density of the reacting species and temperature which in turn affect the rate of the photochemical reaction responsible for airglow process. In summary, the perturbations due to passage of gravity waves or tides are reflected as wavelike modulations in the airglow emission intensity. After the advent of CCD based detectors and the advances in

observational techniques, the imaging observations have proved an excellent tool to study the propagation characteristics of the small-scale gravity waves and their temporal evolution during recent times (due to the fact that the sequential images captured by an imaging system provide excellent track of gravity-wave events). As for example, Medeiros et al. (2005) presented a comprehensive report on the horizontal characteristics of gravity waves observed over three different locations in South America. Wrasse et al. (2006) studied the gravity wave propagation through atmosphere using imaging observations and reverse ray-tracing technique. Also, several reports now exist on the detection of planar wave fronts and non-linear wave events such as mesospheric bores and wall identified with the help of airglow imaging (Shiokawa et al., 2000; Smith et al., 2006; Scheer & Reisin, 2010).

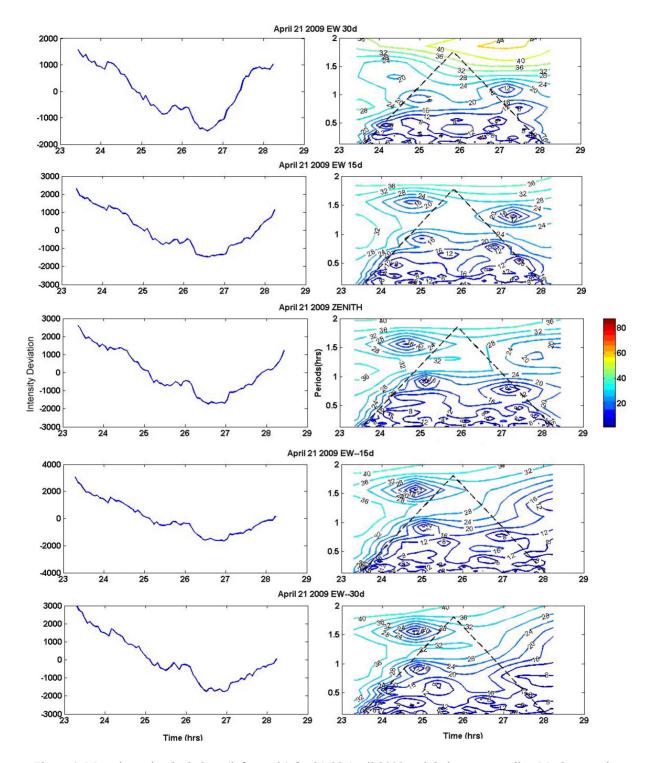
With reference to such studies in Indian subcontinent, there had been isolated studies of gravity waves at the MLT heights with simple airglow photometers (Taori & Parihar, 2011; Taori et al., 2012b) and airglow imagers (Mukherjee et al., 2010; Lakshmi Narayanan et al., 2010). Using imaging observations, Mukherjee et al. (2010) studied the effects of wind filtering on the propagation of gravity waves over Allahabad (25.5° N, 81.9° E), India; and Lakshmi Narayanan et al. (2010) presented the observations of large- and small-scale gravity wave features in OH nightglow images associated with the convective instability over Tirunelveli (8.7° N, 77.8° E). Using nightglow photometry, Parihar et al. (2011) reported the observations of gravity waves and tides in OI 557.7 nm emission intensity and OH temperatures; while, Taori et al. (2012b) reported the observations of gravity waves in 45-90 km altitude regime over Gadanki (13.8° N, 79.2° E), India using simultaneous airglow and Rayliegh lidar measurements. However, the simultaneous measurements of horizontal wavelengths and periodicity of gravity waves have not been reported till now. Motivated by this fact, a case study of airglow imaging observations carried out on 21-22 and 23-24 April 2009 from Allahabad (25.5° N, 81.9° E), India has been made, and this report constitutes probably the first one featuring concurrent measurements of horizontal wavelengths and periodicity. Gravity wave activity was stronger on these two nights compared to the other nights during April 2009.

2. Experimental Set Up, Results and Discussion

An all sky airglow imaging system (manufactured by Keo Scientific Ltd., Canada) was deployed for observations of OH nightglow at Allahabad (25.5° N, 81.9° E), India. The imaging system comprises a fast f/4 all-sky telecentric lens systems (having field of view of 179°) as the optical unit, and a back-illuminated 512 x 512 pixels CCD (Scientific grade 1, 24 μ m x 24 μ m, and thermoelectrically cooled to -53° C) as the photon detector. WinView software was used to control the camera. A 190 nm broadband optical filter (720-910 nm) [having a transparency of 87 % and a notch at 868 nm {to exclude contribution from the $O_2(0, 1)$ Atmospheric band emission] thermoelectrically cooled at -25° C was used to monitor OH nightglow. Although the imager had six filters, one filter could be only operated due to software limitation. On 21-22 April 2009, the exposure and delay time was adjusted to have a cycle of 4 min, whereas, it was 2 min for 23-24 April 2009. The image processing involved a) the flat-field corrections to account for the intensities variations due to the lens curvature, b) to approximately remove the artifacts due to van Rhijn effect and atmospheric extinction c) the non-uniform pixel-to-pixel sensitivity of the CCD detector, and d) scaling to 5 % to 95 % of the intensity range. Assuming the OH emission peak to be 87 km and it remained unchanged during the night, the images were transformed to geographic coordinate system. In order to identify the short period wave features (mainly horizontal scales and periodicity) – firstly, the average intensity of a square bin of 16 pixel x 16 pixel of the processed image was computed along zenith, 15° North, 15° East and 15° West; and then using this intensity information, the time series were generated for zenith and different off-zenith directions. This was followed by the calculation of the intensity deviation at a particular time by substracting the mean value during the night from the observed intensity, so as to construct a detrended series, and then Morlet wavelet analysis of this series was performed (see Torrence and Compo, 1998 for more information on Morlet wavelet analysis) to identify the harmonics present in the nightglow data as well as their phase information.

2.1 Observations of 21-22 April 2009

The intensity deviations (left panels) and corresponding Morlet wavelet analysis (right panels) for OH nightglow measurements on 21-22 April 2009 are shown in Figure 1. In the figure, the variability observed along zenith angles varying from 30° E to 30° W at 15° interval (representing the zonal intensity variability) are plotted from top to bottom. In each plot, the signatures of short period oscillations riding over a long period nocturnal variation can clearly be seen. It is important to note here that along 30° E, the nocturnal plot shows the intensity minima to occur at about 26.7 h (i.e. 02.7 h IST of 22 April 2009) while the plot along 30° W shows minima occurring near 27.0 h (i.e. 03.0 h IST of 22 April 2009) which clearly indicates the propagation of waves. The wavelet analysis of the intensity data reveals the presence of three distinct wave packets of a) 0.4-0.5 h wave, b)



0.7-1.0 h wave and c) 1.1-1.5 h wave. Please note that the dotted black lines in the wavelet analysis represent the cone of influence.

Figure 1. Mean intensity deviations (left panels) for 21-22 April 2009 and their corresponding Morlet wavelet analysis (right panels). Plotted from top to bottom are the mean intensity deviations for zenith angles 30° E to 30° W at 15° interval

To study the short period gravity wave feature and their zonal and meridional structures, we follow the phases of wave packets observed in the wavelet spectra. We categorize three wave packets as stated above and find out the

time of maximum amplitudes of individual wave packet spectra and utilize this information to estimate their structures in zonal as well as in meridional direction. For example, 0.4-0.5 h wave show maximum of wave amplitudes (in wavelet spectra) to occur at about 24.1, 24.3, 24.5 and 24.2 h IST for 30° E, 15° E, Zenith, 15° W and 30° W respectively, while; the 0.7 - 1.0 h wave show the maximum of amplitudes to occur at 24.4, 25, 25.1, 25 and 24.9 h IST for zenith angles 30° E to 30° W at 15° interval (please note that time is in continuation from the observations and therefore 24.4 h means 0.4 h IST of next day, and so on). Utilizing this information, we plot the phase of waves in Figure 2 (shown in solid squares). One may clearly see signature of wave structures in the data. To emphasis the wave structure in data, we perform a simple best-fit waveform analysis. In this analysis, a simple best fit cosine model of the following form is applied on the detrended data to determine the perturbation amplitudes:

$$Y = Y_0 + A^* \cos[\pi (X - Xc)/W]$$
⁽¹⁾

where, Y_0 is the mean values (which is 0 in our case), A is the amplitude of the fitted wave of half-wavelength W with phase Xc, and X is the space. The results of the best-fit analysis for zonal scans are shown as red solid connecting lines. One may note clearly that the 0.4-0.5 h waves have a zonal wavelength of ~126 km. For 0.7-1.0 h waves the horizontal wavelengths could not be estimated due to unclear wave-form (possibly because their horizontal wavelengths may be larger than the field of view of imager). The 1.1-1.5 h wave packet on the other hand shows the horizontal wavelengths to be ~90 km.

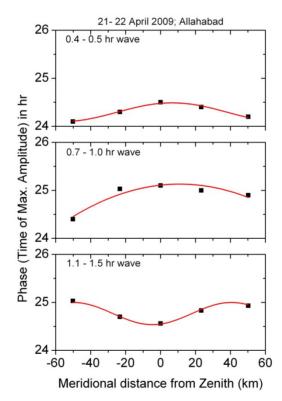
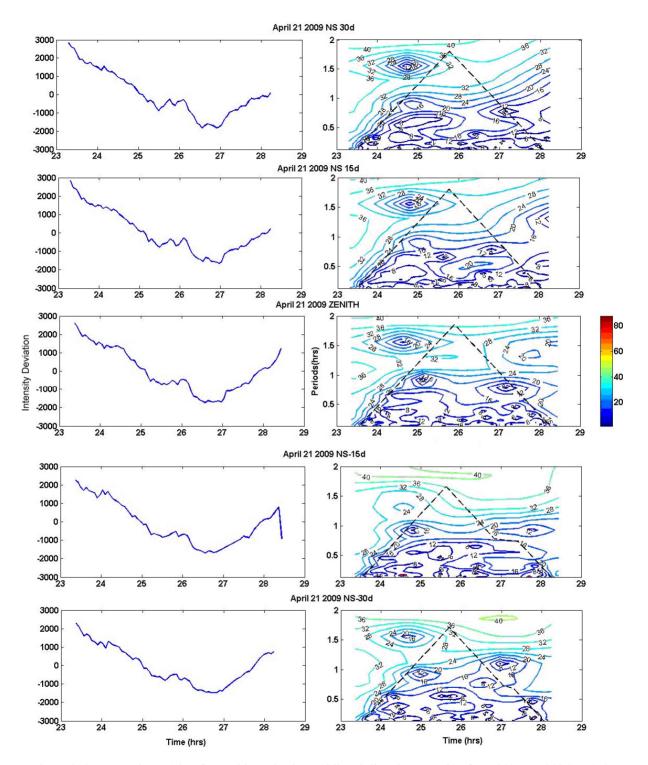


Figure 2. The phases of waves as noted in the wavelet analysis together with the best-fit cosine model analysis for zonal positions corresponding to zenith angles 30° E to 30° W at 15° interval

The intensity deviations in the meridional direction (zenith angles, 30° N, 15° N, 0°, 15° S and 30° S) are shown in the left panels of Figure 3, while the corresponding wavelet analysis is shown in right panels. In general, the long period nocturnal variation, which exhibits minima about 2700 h, i.e. 0300 IST shows a slow progression from North to South. To find out the meridional structures in the observed short period waves, we first categorize three wave packets (as explained earlier) of 0.4-0.5 h, 0.7-1.0 h and 1.1-1.5 h periodicity band and plot the time of maximum amplitudes of these wave packets in Figure 4 (filled squares). The absence of a data for 0.4-0.5 h wave at around 22.5 km is because of unclear signature of this wave at 15° S. Results of the best-fit cosine model which are shown as red connecting lines in Figure 4 are utilized to get an estimate on the horizontal scales of these wave packets. One may note clear signatures of waves with meridional wavelengths 72, 199 and 106 km



for 0.4-0.5 h, 0.7-1.0 h and 1.1-1.5 h waves respectively. Table 1 summarizes the observed wave features for this particular night.

Figure 3. Same as Figure 1 but for zenith angles in meridional directions varying from 30° N to 30° S at 15° interval for 21-22 April 2009 data

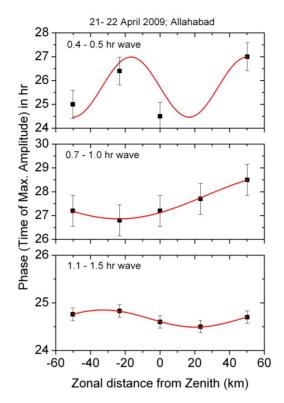


Figure 4. Same as Figure 2 but for zenith angles varying from 30° N to 30° S at 15° interval for 21-22 April 2009

Table 1. Summary of the observed harmonics present along zenith and different of zenith directions along with the time of maximum phase (here τ correspond to the periodicity of the observed wave, while the time of maximum phase is represented by t_m) for 21-22 April 2009

	1st wave		2nd wave		3rd wave		4th wave		5th wave	
Directions	τ	t _m								
	(h)	(IST)								
Zenith			1.55	24.56	0.90	25.10	0.77	27.16	1.31	27.80
15° N			1.55	24.83	0.60	25.60	0.70	26.80	0.50	26.40
15° S			1.31	24.50	0.90	24.76			0.90	27.76
15° E	0.46	24.30	1.50	24.70	0.92	25.03	0.70	26.80	1.30	27.30
15° W			1.55	24.83	0.90	25.00	0.77	26.96		
30° N			1.55	24.76	0.60	24.96	0.77	27.16		
30° S			1.55	24.70	0.92	24.90	0.70	28.56	1.10	26.96
30° E	0.40	24.10	1.30	24.40	0.90	25.03	1.10	27.10	0.70	27.50
30° W			1.55	24.93	0.90	24.90	0.65	25.40		

2.2 Observations of 23-24 April 2009

Figure 5 presents the intensity deviations and the results of wavelet analysis for 23-24 April 2009. The variations observed on this particular night were dominated by short period wave structures. The longer period nocturnal variations show minima to occur at around 2200-2300 h IST at all the zenith angles emphasizing the presence of a tide-like wave in the data. The left panel in Figure 5 plots the mean intensity deviations in zonal direction for zenith angles 30° E, 15° E, 0° , 15° W and 30° W (from top to bottom), while the right panels show their corresponding wavelet spectra. One may note larger amplitudes of short period waves on this night compared to 21-22 April 2009. Also, in the wavelet spectra one may note clear signatures of wave phases to occur at different

times for the data obtained at different zenith angles. Although, one can clearly note a phase propagation of waves in the data; as explained earlier, we carry out the best-fit analysis on the wave phases (time of maximum amplitudes) to estimate the zonal structures of observed waves in the data. Results of the best-fit analysis are shown in Figure 6. In this figure, solid squares show the observed phase of waves at 30° E, 15° E, Zenith, 15° W and 30° W while, the solid red connecting lines show the best-fitted model. The results reveal that 0.4-0.5 h wave has a horizontal wavelength of ~ 61 km, while the 0.7-1.0 h and 1.1-1.5 h waves have their horizontal wavelengths ~97 km and 105 km respectively.

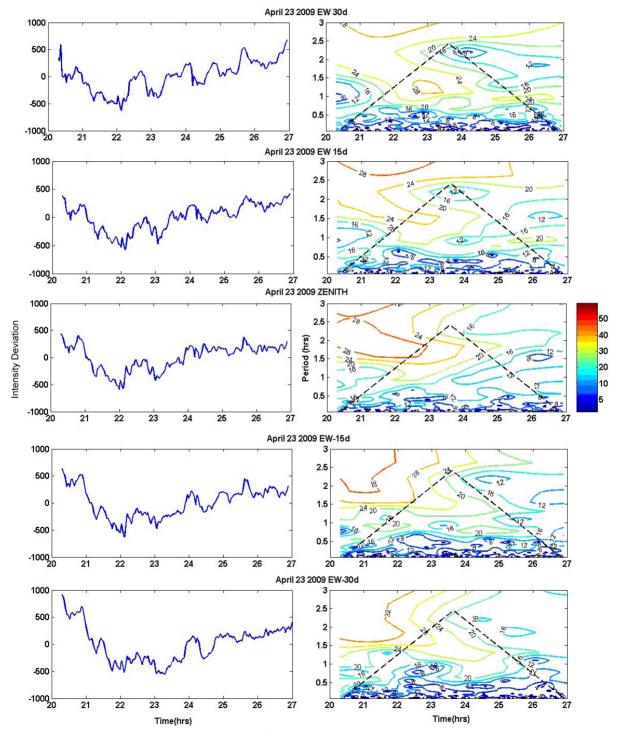


Figure 5. Same as Figure 1 but for the observations carried on 23-24 April 2009

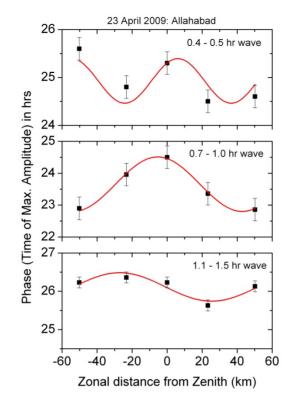


Figure 6. Same as Figure 2 but for the observations carried on 23-24 April 2009

The observed mesospheric OH intensity variability in meridional direction is shown in the left panels of Figure 7. Similar to the variability observed in the zonal direction, the long period tide like wave is noteworthy in data with minima at around 2200-2300 h IST. One may also note the similar wave modes extending from 30° N to 30° S zenith angles. The right panels depict the results of wavelet analysis of the mean intensity deviation data. The short period wave features with periodicity 0.25 to 1.5 h are clearly noted in the data with their phase varying with zenith angles. For an estimation of meridional structures of waves, we plot the phase of wave packets with zenith angles in Figure 8 as solid squares. The best-fit cosine model results are shown as connecting red lines. The horizontal wavelengths in meridional directions are estimated to be ~ 105 km, 55 km and 80 km respectively for 0.4-0.5 h, 0.7-1.0 h and 1.1-1.5 h waves. Table 2 summarizes the observed wave features for this particular night.

Table 2. Same as Table 1 but for 23-24 April 2009

	1st wave		2nd wave		3rd wave		4th wave		5th wave	
Directions	τ	t _m								
	(h)	(IST)								
Zenith			0.30	22.93			0.46	25.30	1.55	26.23
15° N	1.10	21.13	0.92	23.20	2.20	24.03	1.10	25.50	1.50	26.26
15° S			2.20	22.96	1.45	23.23	1.10	25.60	0.77	26.23
15° E	0.65	22.10	2.20	23.76	0.93	23.97	0.55	24.80	1.55	26.36
15° W	0.92	21.70	0.77	24.50	0.92	23.36	2.20	24.80	1.10	25.63
30° N	0.77	21.50	2.20	23.53	0.40	23.26	0.70	26.10	1.10	26.40
30° S	1.85	22.06	0.40	22.10	0.55	23.63	0.92	24.50	1.13	26.60
30° E	0.55	22.80	1.31	22.96	2.20	24.16	0.46	25.66	1.85	26.23
30° W	0.90	22.86	0.30	24.46	2.26	24.50	1.85	25.50	1.10	26.13

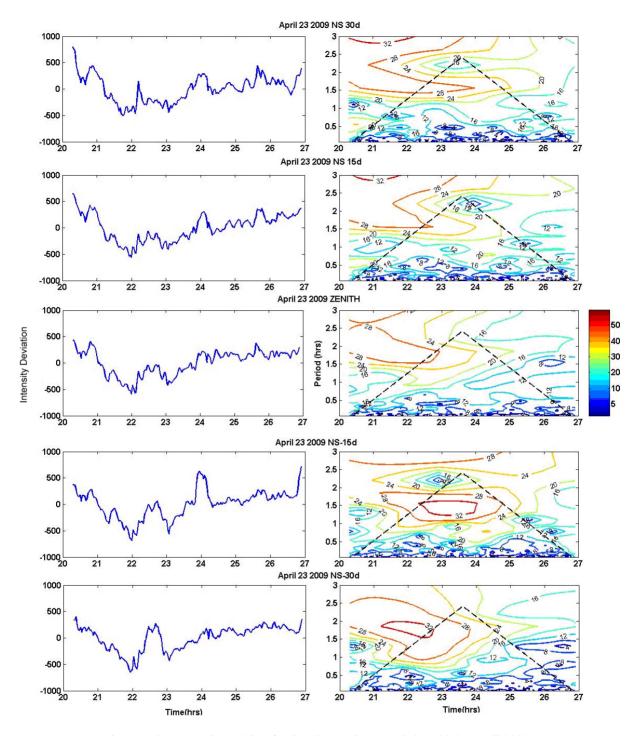


Figure 7. Same as Figure 3 but for the observations carried on 23-24 April 2009

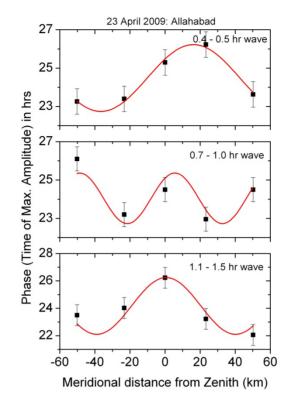


Figure 8. Same as Figure 4 but for the observations carried on 23-24 April 2009

It is important that the short period waves observed on 21-22 April 2009 as well as 23-24 April 2009 exhibit zonal as well as meridional structures. With aircraft-borne Michelson Interferometer measurements, it has been shown the zonal as well as meridional wavelength associated with short period gravity waves to be $\sim 41, 65$ and 230 km in meridional directions (Espy & Huppi, 1997). Our observations are important in terms of zonal momentum exchanges (Sato et al., 1999). It is well appreciated that the thermal structure (apart from the radiative balance) in the upper mesosphere is explained mainly by the existence of meridional circulation due to the gravity wave induced forces. The gravity waves propagating purely meridionally do not associate with vertical flux of zonal momentum, although they have a role in the momentum balance in the middle atmosphere. The waves observed in present investigation show zonal as well as meridional structures and as the meridionally propagating waves with non-zero zonal components are important for the meridional distribution of vertical flux of zonal momentum (Sato et al., 2003), the present observation has an importance. This is further substantiated because the departure from the gradient-wind balance may possibly due to the dissipation of gravity waves and tides with associated vertical flux of meridional component (Liberman, 1999). Although the present study is a limited attempt; a wider study is in progress to achieve a suitable statistics on the short period waves and their zonal and meridional structures which will be important for the global circulation of middle and upper atmosphere.

3. Conclusions

Imaging observation of OH nightglow has been made at Allahabad (25.5° N, 81.9° E), India during April 2009. In understanding the role that gravity waves play in the MLT dynamics, the observations of zonal and meridional structure of short-period gravity waves are considered important. Herein, the concurrent measurements of horizontal wavelengths and periodicity of gravity waves on two nights (viz. 21-22 and 23-24 April 2009) has been presented. Morlet wavelet analysis of the intensity data was performed to identify the wave packets present in the data, and mainly three distinct wave packets having period in the range of (i) 0.4-0.5 h, (ii) 0.7-1.0 h and (iii) 1.1-1.5 h were present. The horizontal wavelength of these observed wave packets lay in the range of 55-199 km. In the South American sector, Medeiros et al. (2005) found the horizontal wavelength varying from 15 to 35 km, while Wrasse et al. (2006) reported the horizontal wavelengths ranging between 5 and 30 km for 5-10 minute waves. In future, a comprehensive study featuring short-period gravity waves will be performed with a bigger database encompassing several nights to understand the gravity wave-MLT circulation interconnection.

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