A Generic Tool for Teaching Compilers

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Abstract

In this paper, we propose a two-fold generic tool for compiler construction. First, it facilitates teaching compilers. Second, it constitutes a new approach for compiler construction. In addition, it enables a smooth transition from theory to practice and introduces a unified approach for the implementation of the different compiler phases. Such unification is achieved based on the representation of the compiler phases as a generic domain that is then mapped into a generic automaton. The generic automaton simulates the behavior of finite and shift-reduce automata, annotated by respective translation schemes. Thus, the tool acts as a scanner, a parser or as syntax directed translator. Without loss of generality, the proposed tool is used within a compiler-teaching framework. Comparisons with similar and well-known approaches have shown that our approach is pedagogical, conceptually simpler, requires less student efforts and more relevant to core curriculum.

Keywords: teaching framework, scanning, parsing, grammars, syntax directed translation

1. Introduction

In this paper, we propose a generic tool for teaching compilers. Usually, compiler construction is taught as a one-semester course having as prerequisites courses in programming languages; data structures and computer organization. Within the framework of the compiler construction course, the students are requested to write a compiler from a given language specification, using automated tools such as Lex and Yacc (Mason & Brown, 1990). However, such teaching approach loosely-couples the theory of scanning and parsing. In addition, it constitutes an ambiguous shift from theory to practice, associated by the inherent difficulties and the typical errors of automated tools (Mallozzi, 2005). Hence, in this paper we set an objective to tightly couple scanning, parsing and translation, as well as to keep a connection and a smooth transition between theory and practice.

Such coupling is based on a proposed generic tool for the construction of scanners, parsers, and syntax directed translators. The proposed tool is used as a unifying tool within the following framework for teaching compilers

1) Introduce compilation, including its different phases.

2) Introduce regular expressions and context-free grammars. Emphasize their roles in specifying the lexical and syntactic levels of high level programming languages.

3) Introduce scanning in terms of finite automata. Emphasize the role of automata as scanners of languages specified by regular expressions (definitions).

4) Introduce parsing in terms of push down storage automata. Emphasize the role of automata as parsers of languages specified by context free grammars.

5) Introduce the concepts of a generic grammar that can be instantiated either by regular expressions and context-free grammars. Emphasize its role in constructing a generic automaton (scanner-parser).

6) Construct the generic automaton as a scanner.

7) Construct the generic automaton as a parser.

8) Introduce the concepts of the syntax directed translation. Emphasize the role of the translation schemes.

9) Consider the remaining compilation phases in their subsequent order. Extend the automaton as type-checker, intermediate code generator and as code generator.
The outlined framework is consistent with ACM’s Curriculum 2001. It is motivated by the strategies and the teaching approaches suggested in (Aho, 2008; Waite, 2006). However, the proposed framework adopts a unified approach for teaching theory and its practical application. Such unification is achieved by adopting a generic grammar that can be either instantiated by context-free grammars or by regular definitions. Such grammar is annotated by appropriate translation schemes. As such, the augmented grammar is then transformed into an augmented generic automaton (AGA). The states and the transitions of AGA are defined based on combining concepts from LR automata, finite automata, with embedded translation schemes (Aho et al., 2007). Hence, the parsing behavior of AGA is generic. It simulates finite automata, shift–reduce automata and syntax directed translator. However, AGA is a nondeterministic. It is efficiently transformed into a reduced one, called RAGA, using a proposed subset construction approach. In addition, the subset construction produces parsing and translation tables that specify the RGA parsing/translation actions, respective a given state and each one of the input symbols. A simulator is then constructed to simulate the run (scanner/parser/translator) of RGA on strings derived from a generic grammar.

Our parsing approach is based on position parsing automata (PPA), as proposed in (Jabri, 2009, 2012). However, it extends PPA to act as a scanner/parser/translator and uses different construction approach that handles recursion by reduced stack activities in a way similar to the generalized bottom up parsers and the reduction-incorporated parsers, as proposed in (Ayock, 2001; Johnstone & Scott, 2007; Scott & Johnstone, 2005) respectively. In addition, it handles nondeterminism in a way similar to SLR parsing as proposed in (Jabri, 2012).

The remainder of this paper is organized as follows. Section 2 presents preliminaries. Section 3 presents the proposed generic tool and the respective algorithms for its implementation. Section 4 presents experimental results, followed by a discussion and a conclusion that are given in Section 5 and Section 6 respectively.

2. Preliminaries

For our further discussions, we assume the following definitions based on the ones given by Aho et al. (2007) and by Jabri (2012). These definitions are used to specify the subsequent phases of a compiler as follows:

- The specification needed for lexical analysis and parsing are based on regular definition and context free grammars as given in Definition 1 and Definition 2 respectively. A unified definition for both is based on a generic grammar as given in Definition 3.

- The specification needed for the remaining compiler phases are based on syntax directed translation schemes (Aho et al., 2007) where program fragments are embedded within the productions of the generic grammar. These fragments are enclosed between braces ( {...}) and denoted as translation schemes.

**Definition 1.** Given an alphabet \( \Sigma \), a regular expression (RE) is defined as a notation to describe all languages that can be built from the symbols of \( \Sigma \) by applying the operations: union (\( | \)), concatenation (\( . \)) and exponentiation (\( * \)). RE is then inductively defined as follows:

- The symbol \( \varepsilon \) is RE if \( x \in \Sigma \) then \( x \) is RE.
- Let \( x, y \) be RE. Then RE is inductively defined as: \( xy \) is RE; \( x | y \) is RE; \( x^* \) is RE and (\( X \)) is RE.

**Definition 2.** Given an alphabet \( \Sigma \), a regular definition (RD) is a sequence of definitions of the form: \( RD_1 \rightarrow RE_1 \), \( RD_2 \rightarrow RE_2 \), ..., \( RD_n \rightarrow RE_n \), where \( RD_i \in \Sigma \) and \( RE_i \) is defined over \( \Sigma \cup \{ RD_1, RD_2, ..., RD_n \} \).

**Definition 3.** An Action-annotated Generic Grammar is defined by the 5-tuple \( AGG = (\Sigma, N, P, S, TS) \) that is either instantiated by a context free grammar (CFG) or by RD. In addition, it is annotated by translation schemes to specify a particular translation as follows:

1) AGG is instantiated by CFG, if:
- \( \Sigma \) is an alphabet of terminal symbols.
- \( N \) is a finite set of nonterminal symbols, where \( S \in N \) is a starting symbol.
- \( P \) is a finite set of productions \( p \) having the form \( A \rightarrow V \), where \( A \in N \) and \( V \in (\Sigma \cup N) \).
- \( TS \) is set of translation schemes to specify particular translation phase, where the individual productions are annotated by such schemes as in \( p: A \rightarrow V:: \{ \) translation scheme \( \} \).
2) AGG is instantiated by RD, if:

- $\Sigma$ is an alphabet of symbols.
- $N = \{RD_1, RD_2, ..., RD_n\} \cup OP$, where $\{RD_1, RD_2, ..., RD_n\}$ is an ordered set of nonterminal symbols; $S \in N$ is a starting symbol and OP are special nonterminals representing the operations: $|$, $( )$, $(.)$ and $\ast$.
- $P$ is a finite set of productions $p$ having the form $A_i \rightarrow R_i$, where $A_i \in \{RD_1, RD_2, ..., RD_n\}$ and $R_i$ defined by applying OP over ($\Sigma \cup \{RD_1, RD_2, ..., RD_n\}$).
- $T$ is a set of translation schemes to specify the translation of lexical entities into appropriate tokens as in $p: A_i \rightarrow R_i :: \{ \text{translation scheme} \}$.

Subsequently, in our further discussion, we use a string as a generic term to either denotes strings, generated by RD, or sentences generated by CFG. These strings are annotated by appropriate translation schemes.

Example 1. Let $G = (\Sigma, N, P, S, TS)$ be AGG instantiated by RD, where: $(a-z, 0-9, +, *) \in \Sigma$, $(Id, num, op, ws, token, tokenlst) \in N$, $P = \{ \text{letter} \rightarrow a | b | ... | z, \text{digit} \rightarrow 0 | ... | 9, \text{ws} \rightarrow \text{blank}, id \rightarrow \text{letter (letter | digit)}, \text{num} \rightarrow \text{digit (digit)}, \text{op} \rightarrow + | \ast, \text{token} \rightarrow \text{id | num | op, tokenlst} \rightarrow \text{tokenlst ws token} \}$ and $TS$ is a set of translation schemes. Examples for strings generated by $G$ are: xy2z, 23.5 and 56.9. A possible annotation of $G$ is as follows:

- $id \rightarrow \text{letter (letter | digit)} :: \{ \text{Return (ID)} \}$, where ID is an encoding of a token of type id; $\text{num} \rightarrow \text{digit (digit)} :: \{ \text{Return (NUM)} \}$, where NUM is an encoding of a token of type num and $\text{op} \rightarrow + | \ast :: \{ \text{Return (OP)} \}$, where OP is an encoding of a token of type op.

Example 2. Let $G = (\Sigma, N, P, S, TS)$ be AGG grammar. It is instantiated by CFG as follows: $\Sigma = \{id, +, \ast\}$, $N = \{E, T, F\}$, $P = \{ E \rightarrow E + T | T, T \rightarrow T*F | F, F \rightarrow id \}$ and $TS$ is a set of translation schemes. Examples for strings generated by $G$ are: id*id, id, and id +id*id. A possible annotation of $G$ for type checking is as follows:

- $\text{F} \rightarrow \text{id} :: \{ \text{Type.F = Type.id} \}$ and $\text{E} \rightarrow \text{E + T :: Type.E = f(Type.E, Type.T)}$.}

3. The Proposed Generic Tool

Let $G = (\Sigma, N, P, S, TS)$ be an AGG grammar. The proposed generic tool (GCT) is defined either as a scanner, if $G$ is instantiated by RD, or as a parser, if $G$ is instantiated by CFG. In addition, GCT is defined in away that permit its transformation to a translator respective to the translation schemes (TS), annotating the individual productions of $G$. As such, GCT has the structure shown in Figure 1, where:

\[
\text{AGG} \rightarrow \underline{\text{Construction Algorithm}} \rightarrow \text{AGA} \rightarrow \underline{\text{Subset Construction}} \rightarrow \text{RAGA}
\]

![AGG structure](image)

- AGA is a nondeterministic automaton defined and constructed as given by Definition 4 and Section 3.1.
- RGA is a reduced automaton obtained as a result of applying a subset construction on AGA as given in Section 3.2.
- A simulator for RGA constructed as given in Section 3.3. Such simulator acts either as a scanner/translator or a parser/translator.
- Once a string is fed as an input to RGA simulator, an output is then produced as consisting of a respective sequence of AGG's production reductions and the results of the execution of the translation schemes annotating the individual AGG's productions.

Definition 4. An Augmented Generic Automaton (AGA)

Let $(\Sigma, N, P, S, TS)$ be AGG grammar. AGA is then defined by the 5-tuple $((\Sigma \cup \epsilon), Q, q_{\text{in}}, q_{\text{fin}}, TA)$, where:

- $\Sigma$ represents strings generated by the AGG grammar.
- Each grammar symbol $V \in (\Sigma \cup N)$ is represented by the pair $(V^i, V^f)$ to represent a prediction and an acceptance of $V$ in an assumed translation. Consequently, The GCCT states respective to each $V \in (\Sigma \cup N)$ are defined as the set $\{q' = V^i, q^f = V^f\}$, where: $q'$ is an initial state instantiated by $V^i$ and acts as a predictor (scanner) for $V$. The state $q^f$ is a final one, instantiated by $V^f$ and acts as its respective

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acceptor. In addition and if \( V \) is associated with a translation scheme, the state \( q^f \) is augmented by such scheme as a translation action to be executed upon transition to \( q^f \). Hence, the set of AGA states is defined as \( Q = \{(q^i = V^i, q^f = V^f) \mid V \in (\Sigma \cup N)\} \) where, each state is instantiated by a respective grammar symbols.

- \( (q_{in} = S_i) \) and \( (q_{fin} = S^f) \) are the initial and final states, instantiated by the symbols respective to the starting grammar symbol of the AGG grammar.

- \( TA \) is a set of the translation actions of AGA. It consists of parsing actions annotated by translation schemes. The parsing actions consist of move transitions and reductions. Upon transitions and reductions, the action specified by such scheme is executed as an integral part of the parsing action. The move parsing actions are defined by the set \( SPA = \{\sigma(q_i, V) = (q_j) \mid \{\text{translation scheme}\}\} \), where \( \sigma(q_i, V) = (q_j) \) specifies a subsequent state \( q_j \in Q \) for a given state \( q_i \in Q \) and a given grammar symbol \( V \in T \). Upon transitions, a program fragment is performed as indicated by the annotating translation scheme. The reduce parsing actions are defined by the set \( RPA = \{\delta(q, V) = \text{reduce}(r) \mid \{\text{translation scheme}\}\} \), where \( \delta(q, V) = \text{reduce}(r) \) defines a reduction rule \( r \) for every \( V \in N, q \in Q \) such that \( q \) has been instantiated by \( V^f \) and \( V \) is the LHS \((r)\). RPA performs the indicated \{translation scheme\}. If the reduction is associated with such scheme.

The states and the parsing actions of AGA are dependent on the production types; the types of the grammar symbols and their respective positions in the individual productions of AGG, They are inductively constructed as given in Section 3.1.

### 3.1 AGA Construction Approach

Let \( G = (\Sigma, N, P, S, TS) \) be an AGG grammar, where:

- \( G \) is either instantiated by CFG or RD. Respectively, the set of productions \( P \) is generic and is either instantiated by grammar productions or regular definitions.
- The productions of CFG are classified into three types: simple productions, productions having alternatives and productions having embedded recursion.
- Given \( p \in P \), the grammar symbols \( V \) in \( p \) are classified into the following types: terminals, ranked terminals, nonterminals, a recursive-head (\( V \) is LHS \((p)\) and \( p \) is a production having embedded recursion) and a recursive-instance (\( V \in RHS(p) \) and \( V \) is LHS \((p)\)). In addition, each nonterminals with repeated occurrences in RHS of different productions is classified as repeated–instance.
- The right hand side of RD are regular expressions on which the following operations are applied: Concatenation; alternation; exponentiation.
- Considering a particular compilation phase, respective translation schemes (TS) are defined and used to annotate the set \( P \).

Assuming that the right hand sides (regular expressions) of RD are decomposed into their constituent sub expressions, Algorithm 1 constructs AGA for RD (AGA (RD)) as well as for CFG (AGA (CFG)). The construction of AGA (RD) or (AGA (CFG)) proceeds according to the same steps from which Algorithm 1 is composed. However, the construction of AGA (RD) excludes the step covering embedded recursions, while the construction of AGA (CFG) excludes the one covering exponentiation.

**Algorithm 1: AGA Construction Algorithm**

**Input:** An AGG grammar \( G = (\Sigma, N, P, S, TS) \).

**Output:** GA defined by the 5-tuple \( ((\Sigma \cup \varepsilon), Q, q_{in}, q_{fin}, TA) \) and its respective transition graph.

**Method:**

Initially, the states of AGA are constructed as the set as \( Q = \{(q^i = V^i, q^f = V^f) \mid V \in (\Sigma \cup N)\} \). AGA is then inductively constructed as follows:

1. **Basis:**
   - Let \( (q_i, q_f) \in Q \) be an arbitrary states, denoted as an initial state and a final one respectively, AGA for the grammar symbol \( \varepsilon \) (AGA (\( \varepsilon \))) is then constructed as shown in Figure 2.
Figure 2. AGA (ε)

It constitutes an ε-transition (σ(qi, ε) = (qf, ::{ translation scheme}) between qi and qf, associated with a translation scheme.

- Let V ∈ Σ, AGA (V) is then constructed as consisting of two states (Fig.3) with the following transitions σ(qi, V) = (qf) ::{ translation scheme}

![Figure 3. AGA (V)](image)

2) Induction:

2.1 Let p ∈ P: LHS(p) → RHS(p) be either a simple production or a concatenation of subexpressions; AGA (p) is then constructed as shown in Figure 4.

![Figure 4. AGA (p)](image)

where: qi is the initial state and qf the final state of AGA (p). AGA (RHS(p)) is an aggregation of AGA1, …, and AGAn respective to the individual grammar symbols from which RHS (p) is composed. Hence, it is constructed as shown in Figure 5.

![Figure 5. AGA (RHS(p))] (image)

Each AGAi has qi and qf as an initial and final states respectively. AGA(p) has the following translation actions:

SPA: σ(qi, ε) = (qi) ::{ translation scheme}, where qi is an initial state of AGA (RHS(p)).

SPA: σ(qf, ε) = (qf) ::{ translation scheme} where qf is the final state of AGA (RHS(p)).

SPA: {σ(qi, ε) = (qi+1) ::{ translation scheme} | i=1,…, n-1 }.

RPA: δ(qf, LHS(p)) = reduce (LHS(p)) ::{ translation scheme}.  

2.2 Let p ∈ P: LHS(p) → RHS1(p) |…|RHSn(p) be either a production with alternative right hand sides or alternative subexpressions RHS1(p), RHS2 (p),…, RHSn(p). AGA (p) is then constructed as shown in Figure 6.
Each alternative RHS_\_i (p) has a respective AGA(RHS_\_i (p)) with initial and final states q_\_i^i and q_\_i^f respectively. The initial and the final states of AGA (p) are q_i and q_f. AGA(p) has the actions:
SPA: \{ \sigma (q_\_i^i, \epsilon ) = (q_\_i^j) ::\{ translation scheme\} | j=1,..n\}, where q_\_i^j is the initial state of AGA_j.
SPA: \{ \sigma (q_\_i^f, \epsilon ) = (q_\_i^\_f) ::\{ translation scheme\} | j=1,..n\}, where q_\_i^\_f is the final state of AGA_j.
RPA: \delta (q_\_i, LHS(p)) = reduce (LHS(p)) ::\{ translation scheme\}.

2.3 Let p \in P: LHS(p) \rightarrow RHS(p) be a production having embedded recursion, where LHS(p) \in RHS(p) at position ( i ). AGA is constructed as shown in Figure 7.

AGA(p) consists of: the initial state q_i, the final state q_f and the AGA respective to (RHS(p)).
AGA(RHS(p)) has the states q_\_i^i, ..., q_{i-1}^i, q_{i-1}^\_f, q_i^i, q_i^\_f, ..., q_n^f, where q_\_i^i and q_n^f are the initial and final states; q_{i-1}^i and q_{i-1}^\_f are the initial and final respective to the embedded recursion. AGA actions are as follows:
SPA: \{ \sigma (q_\_i^i, \epsilon ) = (q_\_i^\_f) ::\{ recursion-initialization 1\}, where\{ recursion-initialization\} is a program segment, executed during parsing, that creates a stack (q_i) initialized with the symbol \epsilon at the top.
SPA: \{ \sigma (q_n^f, \epsilon ) = (q_f) ::\{ translation scheme\} \}
SPA: \{ \sigma (q_{i-1}^\_f, \epsilon ) = (q_{i-1}^i) ::\{ translation scheme\} \}
SPA: \{ \sigma (q_{i-1}^i, \epsilon ) = (q_i) ::\{ translation scheme\} ::\{ recursion-initialization 2\}, where\{ recursion-initialization 2\} is a program segment, executed during parsing, that initializes a recursive path with a return address q_{i-1}^\_f, pushed on the top of stack (q_i).
RPA: \delta (q_i, LHS(p)) = reduce (LHS(p)) ::\{ translation scheme\} \cup \{ recursion-termination\}, where\{ recursion-termination\} is a program segment, executed during parsing, that terminates a recursive path by performing an \epsilon-transition to the address at top of stack (q_i), if top( stack (q_i)) \neq \epsilon .
SPA: \{ \sigma (q_{i-1}^i, \epsilon ) = (q_{i-1}^\_f) ::\{ translation scheme\} \}.
2.4 Let \( \{ p \in P : \text{LHS}(p) \rightarrow \text{RHS}(p) \} \) be a set of productions having \((A \in \mathbb{N}) \in \text{RHS}(p)\), where \( A \) is classified as repeated-instance. AGA \((A)\) is then constructed for a selected instance. An AGA for each one of the other instance is constructed following the steps for embedded recursion.

2.5 Let \( p \in P : \text{LHS}(p) \rightarrow \text{RHS}(p) \) be a production (regular definition) having a sub expression \( r^* \) at position \((i)\), where \( r^* \in \text{RHS}(p) \) at position \((i)\). AGA \((p)\) is constructed as shown in Figure 8.

![Figure 8. AGA for regular definitions](image)

AGA \((p)\) consists of: the initial state \(q_0\), the final state \(q_f\) and AGA \((\text{RHS}(p))\) respective to \((\text{RHS}(p)).\) AGA \((\text{RHS}(p))\) has the states \(q_{1}^{i}, \ldots, q_{i-1}^{f}, \text{AGA}(r^*), q_i^{1}, \ldots, q_i^{n}, \) where: \(q_{1}^{i}\) and \(q_{1}^{f}\) are the initial and final states for AGA\((r^*)\); \(q_{i}^{1}\) and \(q_{i}^{f}\) are the initial and final respective to the exponentiation. AGA actions are:

- \(\text{SPA: } \sigma(q_0, \varepsilon) = (q_1^i, ) :: \{ \text{translation scheme} \} \)
- \(\text{SPA: } \sigma(q_i^f, \varepsilon) = (q_i^f, ) :: \{ \text{translation scheme} \} \)
- \(\text{SPA: } \sigma(q_{i+1}^f, \varepsilon) = (q_{i+1}^f, ) :: \{ \text{translation scheme} \} \)
- \(\text{SPA: } \sigma(q_{i+1}^f, \varepsilon) = (q_{i+1}^f, ) :: \{ \text{translation scheme} \} \)
- \(\text{SPA: } \sigma(q_{i+1}^f, \varepsilon) = (q_{i+1}^f, ) :: \{ \text{translation scheme} \} \)
- \(\text{SPA: } \sigma(q_{i+1}^f, \varepsilon) = (q_{i+1}^f, ) :: \{ \text{translation scheme} \} \)
- \(\text{RPA: } \delta(q_f, \text{LHS}(p)) = \text{reduce (LHS}(p)) :: \{ \text{translation scheme} \} \)

**Example 3.** Let \( G = (\Sigma, N, P, S, TS) \) be GAA grammar with simple productions. Where: \((\text{id}, +, *) \in \Sigma, (E, T, F) \in N\) and \( P = \{ E \rightarrow E^+T, T \rightarrow T^*F, F \rightarrow \text{id} \} \). A nondeterministic automaton representing AGA respective to \( G \) is shown in Figure 9.

![Figure 9. AGA for the grammar of Example 3](image)
Example 4. Let $G = (\Sigma, N, P, S, TS)$ be GGA grammar instantiated by regular definitions as given in Example 1. Fig. 10 shows a nondeterministic automaton representing AGA respective to the productions: \text{letter} \rightarrow a | b | \ldots | z; \text{digit} \rightarrow 0 | \ldots | 9; \text{id} \rightarrow \text{letter (letter | digit)}^*; \text{token} \rightarrow \text{id}; \text{and tokenlst} \rightarrow \text{token}.

3.2 RAGA Construction Approach

In this section, we propose a construction approach for the reduced automaton RAGA based on extension of the subset construction algorithms given in (Aho et al., 2007; Jabri, 2012). Such extension is a twofold. First, it covers a wider class of grammars including RD and CFG. Second, it has a deterministic behavior upon the RGAG reduce actions, as well as upon return actions as determined by recursion-termination.

The constructed automaton in (Jabri, 2012) has multiple transitions and respective reductions. In contrast, according to the proposed approach, the sets of follow symbols for the nonterminals are used to determine their respective reduction in a deterministic way, similar to the one adopted for SLR parsers (Aho et al., 2007). Based on such approach a proposed algorithm, denoted by Algorithm 2 is given below. Having the AGA states $Q_{AGA}$ and their respective translation actions $TA_{AGA} = \{\text{AGA.PAS, AGA.PAR}\}$ as an input, Algorithm 2 constructs RAGA respective to the nondeterministic one. RAGA (G) is represented by its respective states $Q_{RGA}$ and translation actions $TA_{RGA}$. In its turn, two tables represent $TA_{RGA}$ The first one constitutes a transition table (TRT), where each entry (TRT $[q_i, V_j]$) of such table specifies the transitions of type SPA. The second table RTT specifies the reductions (RPA) and to the translation actions (as indicated by the translation schemes respective to SPA and RPA) to be performed by RAGA (G) during its run on an input alphabet, generated from the grammar G. Thus, Algorithm 2 computes $Q_{RGA}$ using an $\epsilon$-closure function (Aho et al., 2007). This function closes the initial states and the final states respective to the different grammar symbol types. However, it does not close the initial states instantiated by grammar symbols of types recursive-instances ($V_i^i, V_i^f$) and repeated-instance. Algorithm 2 handles these symbols by creating respective states and transitions, including the translation schemes {recursion-initialization} and {recursion-termination}.

Algorithm 2. RAGA Construction

Input: AGA automaton, defined by the 5-tuple: $((\Sigma \cup \epsilon), Q_{AGA}, T_{AGA}, q_{in}, q_{fin})$.

Output: RAGA automaton, defined by the 5-tuple: $((\Sigma \cup \epsilon), Q_{RGA}, T_{RGA}, q_{in}, q_{fin})$. 

Figure 10. AGA for the grammar of Example 4
Method:

Step 1: Construct the set \( Q_{RGA} \) of RAGA states and a respective set \( TA_{RGA} \) of type shift as \( \varepsilon \)-closures of the states in \( Q_{GA} \) and their respective transitions.

Step 2: Complete the construction of the set \( TA_{RGA} \) and construct the respective transition and reduction/translation tables, represented by the tables \( TRT \) and \( RTT \).

Step 1 of Algorithm 1 proceeds by executing the program segment as shown in Figure 11, where it starts by constructing the initial state \( RAGA.q_{in} \) and then repeatedly considers each constructed state \( q \) in \( Q_{RGA} \) to constructs the subsequent states \( q_i \) as \( \varepsilon \)-closure (\( \sigma(q_{pii}, V) \)) such that \( q_{pii} \) in \( q \) and \( \sigma(q_{pii}, V) \in TAGA \). The transitions \( TARGA \) respective to \( q \) are then constructed as \( \sigma(q, V) = q_i \). In addition, it registers the states representing recursion and repetition and constructs \( \varepsilon \)-closures respective to the states initialized by grammar symbols of type \( q_{pi} \). Step 2 of Algorithm 1 proceeds by executing the program segment as shown in Figure 12, where: First, it constructs the transitions respective to the registered-heads as well as the states and transitions respective to the registered-instances. Second, it constructs the reduce/translation actions respective RAGA states and represents these actions (and the RAGA transitions) as entries in the tables \( RTT \) and \( TRT \).

Example 5. Let \( G = (\Sigma, N, P, S) \) be a grammar with simple productions as given in Example 3. \( G \) is annotated by translation schemes to translate expressions in infix notation into ones in postfix notation as given in (Aho et al., 2007). The automaton representing RAGA (\( G \)) as constructed by Algorithm 2 is given in terms of its transition graph and the tables \( TRT \) and \( RTT \) as shown in Figure 13 and Table 1 respectively.

Example 6. Let \( G = (\Sigma, N, P, S) \) be a generic grammar instantiated by regular definitions as given in Example 2.2 but annotated by translation schemes to produce recognized tokens. The automaton representing RAGA(G) as constructed by Algorithm 2 is given in terms of its \( TNT \) and \( TRT \) as shown in Table 2.
For each state $q$ in registered-head
\[
\{ \text{Add } (j, \text{RTT (recursion-initialization)}_1(q)); \text{Add } (\text{RTT}[q, \cdot] = j) \}
\]
For each pair $(q_i^0, q_f)$ in registered-instances
\[
\{ q = \text{Select } (q_i^0, \text{registered-head}); \text{Add } (\text{RTT}[q, \cdot] = q_i^0) \}
\]
For all $V \in \Sigma$ such that ($\sigma(q, V) = q_i) \in \mathcal{T}_{\text{RGA}}$ \{Add (RTT[$q_i^0, V] = q_i\}
\]
\[
\text{Add } (j, \text{RTT(recursion-initialization)}_2(q_f)); \text{Add } (\text{RTT}[q, \cdot] = j);
\]
\}
For each state $q$ in $\mathcal{Q}_{\text{RGA}}$
\[
\{ \text{For each } V \in \Sigma \text{ such that such that } (\sigma(q, V) = q_i) \in \mathcal{T}_{\text{RGA}} \}
\]
\[
\{ \text{Add } (\text{RTT}[q, V] = q_i) \};
\]
For (every $X \in \mathcal{N}$ such that $X' \in q_i$) and (every $V \in \text{Follow } (X)$);
\[
\{ \text{Add } (\delta(q, V) = \text{reduce } r(X) ::= \{\text{translation scheme}\}) \} \text{ to } \mathcal{T}_{\text{RGA}}
\]
\[
\text{Add } (j, \text{RTT } (\mathcal{T}_{\text{RGA}}) (\delta(q, V)) \text{ Add } (\text{RTT}[q, V] = j);
\]
If (X is a recursive-head or a repeated-head)
\[
\{ \text{Add } (j, \text{RTT } (\text{recursion-termination}), \text{Add } (\text{RTT}[q, V] = j)) \}
\]
If (X is a starting symbol) \{Add (j, RTT (Accept), Add (RTT[q, S] = j))\}

Figure 12. The Construction of the RAGA reduce/translation actions and its tables

![Transition Graph of RAGA for the Grammar of Example 5](image)

Figure 13. The transition graph of RAGA for the grammar of Example 5

Table 1. The transition/reduction tables of RAGA for the grammar of Example 5

<table>
<thead>
<tr>
<th>State</th>
<th>Input Symbols</th>
<th>Entry</th>
<th>Action</th>
</tr>
</thead>
<tbody>
<tr>
<td>$q_0$</td>
<td>$q_0$, $q_1$</td>
<td>1</td>
<td>$R (F \rightarrow \text{id}, T \rightarrow F, E \rightarrow T)_i::{(\text{print}(\text{id})), \text{Accept}}$</td>
</tr>
<tr>
<td></td>
<td>$q_1$</td>
<td>2</td>
<td>$R (F \rightarrow \text{id}, T \rightarrow F, E \rightarrow T)_i::{(\text{print}(\text{id})), {(\text{rec-termination})= q_f}$</td>
</tr>
<tr>
<td></td>
<td>$q_2$</td>
<td>3</td>
<td>$R (F \rightarrow \text{id}, T \rightarrow F, E \rightarrow T)_i::{(\text{print}(\text{id})), {(\text{rec-termination})= q_f}$</td>
</tr>
<tr>
<td></td>
<td>$q_3$</td>
<td>4</td>
<td>${(\text{recursion-initialization})}$</td>
</tr>
<tr>
<td></td>
<td>$q_4$</td>
<td>5</td>
<td>${(\text{recursion-initialization})}$</td>
</tr>
<tr>
<td></td>
<td>$q_5$</td>
<td>6</td>
<td>$R (E \rightarrow E+T):{(\text{print}(\text{+})))};\text{Accept}$</td>
</tr>
<tr>
<td></td>
<td>$q_6$</td>
<td>7</td>
<td>$R (E \rightarrow E+T):{(\text{print}(\text{+})))};{(\text{recursion-termination})= q_f}$</td>
</tr>
<tr>
<td></td>
<td>$q_7$</td>
<td>8</td>
<td>$R (E \rightarrow E+T):{(\text{print}(\text{+})))};{(\text{recursion-termination})= q_f}$</td>
</tr>
<tr>
<td></td>
<td>$q_8$</td>
<td>9</td>
<td>$R (F \rightarrow \text{id}, T \rightarrow T<em>F):{(\text{print}(\text{id})), {(\text{print}(\text{</em>})))};{(\text{recursion-termination})= q_f}$</td>
</tr>
<tr>
<td></td>
<td>$q_9$</td>
<td>10</td>
<td>$R (F \rightarrow \text{id}, T \rightarrow T<em>F):{(\text{print}(\text{id})), {(\text{print}(\text{</em>})))};{(\text{recursion-termination})= q_f}$</td>
</tr>
<tr>
<td></td>
<td>$q_{10}$</td>
<td>11</td>
<td>$R (F \rightarrow \text{id}, T \rightarrow T<em>F):{(\text{print}(\text{id})), {(\text{print}(\text{</em>})))};{(\text{recursion-termination})= q_f}$</td>
</tr>
</tbody>
</table>
Table 2. The transition/reduction tables of RAGA for the grammar of Example 6

<table>
<thead>
<tr>
<th>State</th>
<th>Input Symbols</th>
<th>TRT table</th>
<th>RTT table</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>$\varepsilon$</td>
<td>+</td>
</tr>
<tr>
<td>$q_0$</td>
<td>$q_{1r}$</td>
<td>$q_3$</td>
<td>$q_4$</td>
</tr>
<tr>
<td>$q_{1r}$</td>
<td>$q_{1r}$</td>
<td>$q_3$</td>
<td>$q_4$</td>
</tr>
<tr>
<td>$q_{1r}$</td>
<td>$q_2$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$q_3$</td>
<td>$q_3$</td>
<td>$q_4$</td>
<td>$q_7$</td>
</tr>
<tr>
<td>$q_4$</td>
<td>$q_5$</td>
<td>$q_5$</td>
<td>$q_6$</td>
</tr>
<tr>
<td>$q_5$</td>
<td>$q_7$</td>
<td>$q_7$</td>
<td>$q_8$</td>
</tr>
</tbody>
</table>

3.3 RAGA Simulation

Let $G$ be an AGG grammar, respective AGA($G$) and RAGA($G$) are constructed by Algorithm 1 and Algorithm 2. The run of RAGA($G$) on input strings generated by $G$ is then simulated by Algorithm 3, as given below.

Algorithm 3. RAGA Simulator

**Input:** An input string ($w\$)$ and the RAGA($G$) automaton, respective to a grammar $G$. RAGA($G$) is represented by two tables: the transition table TRT and the reduction-translation table RTT.

**Output:** Set of reductions as they occur, if $w \in (G)$ Translation actions as indicated by parsing actions.

**Method:**

Initially, the simulator is in its initial configuration, consisting from the RAGA($G$) initial state $q_{in}$ and the input string, represented as $INPUT[\ ] = w\$. As the individual input symbols are read, the simulator performs their respective parsing actions. This is achieved by executing the following program segment.

```plaintext
NextStates = NextStates \cup \{q_{in}\};
Create-simulation-path (\{q_{in}\});
For each recursive-head $q_{ir}$ in NextStates
{ perform RTT [TRT[q_{ir}]].S (recursion-initialization)};
For $i = 1$ to MaxSize (INPUT)
{Subsequentstates= $\phi$
For each state $q$ in NextStates
{ Movet-states = $\phi$ ; Reduce-states = $\phi$ ; Return-states = $\phi$ ;
  Shift-states = TRT [q, INPUT [i]] ;
  If (Shift-states = $\phi$) { output(Error)}
  Elseif
  {For each state $s$ in Shift-states
   {Movestates = Movestates \cup s;
    Create-simulation-path ( s, simulation-path(q));
    If (s = $q_{ir}$) { perform RTT[[TRT[s, -]].S (recursion-initialization)};
    If (Reduce-state (s))
    { Output (RTT[[TRT[s, LA]].R( reductions);
      Output (RTT[[[TRT[s, LA]].S (translation scheme)
```
If \((s = q_r^i)\) 
\{ Return-states = Return-states ∪ 
( perform RTT([[TRT[s, LA]].S (recursion-termination)]) ; 
\}

Subsequent-states = Subsequent-states ∪ Shift-states ∪ Return-states; 
\}
NextStates = Subsequent-states;
\}

If \((NextStates \cap q_{\text{fin}} \neq \emptyset)\) \{ Accept (Input) \; \}

**Example 7.** Let \(a \cdot c\) be a string generated by the grammar of examples 2.2 and 3.4. The run of RAGA on such string is shown in Table 3.

**Example 8.** Let \(i d \cdot id\) be a string generated by the grammar of examples 2.1 and 3.3. The run of RAGA on such string is shown in Table 4.

<table>
<thead>
<tr>
<th>Table 3. The run of RAGA simulator on a string</th>
</tr>
</thead>
<tbody>
<tr>
<td>Current state</td>
</tr>
<tr>
<td>q0; q1r</td>
</tr>
<tr>
<td>q7</td>
</tr>
<tr>
<td>q8</td>
</tr>
<tr>
<td>q1r; q7r</td>
</tr>
<tr>
<td>q4</td>
</tr>
<tr>
<td>{ R (OP \rightarrow *), {\text{print}(op, *)}, R(T \rightarrow op)}</td>
</tr>
<tr>
<td>q0; q1r</td>
</tr>
<tr>
<td>q7</td>
</tr>
<tr>
<td>q8</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Table 4. The run of RGCCT simulator on a string</th>
</tr>
</thead>
<tbody>
<tr>
<td>Current state</td>
</tr>
<tr>
<td>q0; q1r</td>
</tr>
<tr>
<td>q7</td>
</tr>
<tr>
<td>q8</td>
</tr>
<tr>
<td>q1r; q7r</td>
</tr>
<tr>
<td>q4</td>
</tr>
<tr>
<td>{ R (OP \rightarrow *), {\text{print}(op, *)}, R(T \rightarrow op)}</td>
</tr>
<tr>
<td>q0; q1r</td>
</tr>
<tr>
<td>q7</td>
</tr>
<tr>
<td>q8</td>
</tr>
</tbody>
</table>
4. Experimental Results

To validate the correctness, the simplicity and the applicability of our proposed approach, and in addition, to inspect how easily the transition from theory to practice can be made, the proposed GCT has been assigned as a graduation project. Based on the GCT concepts and its implementation algorithms, the assignment is reduced to the implementation of a version that can be used by students as tool for the construction of the different compiler's phases. The parsing phase has been selected as representative one. As such, GCT has been implemented, using Microsoft Visual C++ 6.0., by the program given in Figure 14, where:

- InteractionContext ( ) is a method to input a AGG grammar defined by the 4-tuple $G = (\Sigma, N, P, S)$. It is implemented by the three functions: Terminals ( ); NonTerminals ( ); and Productions ( ) to facilitate the input of the terminal symbols ( $\Sigma$ ), the nonterminal symbols (N) and the AGG productions (P) respectively. The productions are entered one by one (p), where LHS(p) is entered first followed by the symbols of RHS (p), from left to right. This enables automatic indexing of the grammar symbols by their respective positions within each production. As the productions are entered they are mapped into respective automaton (AGA) states (Q), where for each grammar symbol $V_p$, its corresponding initial state $q_p^i \in Q$ and final state $q_p^f \in Q$ are created.

- Based on the construction algorithm, the method construct_aga( ) completes the construction of the AGA automaton by creating the parsing actions respective to Q. Such construction is achieved using the attached index of the individual states as indicator for the positions of their corresponding grammar symbols within their respective productions. In addition, construct_aga( ) produces as an output the transition graph respective to AGA.

- construct_raga ( ) is a method to construct RAGA automaton according to the subset construction algorithm. It produces as an output the parsing table respective to RAGA.

The outlined implementation of GCT and its use as a scanner/parser/translator have been experimented by the students from three sections of a compiler construction course over three semesters. Several grammars, annotated by respective translation schemes have been used. Compared to previous semesters, the number of students completed their assignments has been increased by 30%. The following is an example of such experiments.

**Example 9.** Considering the grammar $G = (\Sigma, N, P, S)$, where: $(d, b, c) \in \Sigma, (S, A, B, X) \in N$ and $P = \{ S \rightarrow Ad, A \rightarrow BX, B \rightarrow b, X \rightarrow c \}$. Its parsing using GCT proceeds as follows

The grammar G is inputted using an interaction context to enter $\Sigma, N$ and $P$ as shown in Figures 15 and 16 respectively.

The output produced by the method construct_aga ( ) consists of a transition graph of AGA respective to the inputted grammar as shown in Figure 17.
The output produced by the method `construct_raga()` consists of the set of RAGA states and its representative parsing and translation tables as shown in Figure 18, Figure 19 and Figure 20 respectively.

Figure 15. The GCT interaction context to input grammar symbols

Figure 16. The GCT interaction context to input grammar productions

Figure 17. A transition graph of AGA respective to the grammar (3.5) as produced by GCT

Figure 18. The set of RAGA states as constructed by GCT
5. Discussion

The proposed tool has been analyzed and experimented against the set objectives and in two directions. The first one considers GCT as a new compiler construction approach. The second direction considers GCT as a teaching tool.

As a compiler construction approach, GCT has demonstrated the following properties: Generality and soundness of its construction approach. GCT constructs a bottom up parsing automaton (RAGA) that simulates shift–reduce one, but with reduced stack activities. In addition, regular definitions are recognizable by RAGA. Semantic action can be inserted within grammar productions. As a result, GCT can easily provide a syntax directed translator.

RAGA features the finite automata (Aho et al., 2007) in two aspects. The first one is the number of its states transitions. The second aspect is the complexity of its subset construction algorithm. However, these aspects are with additional overhead to handle recursion. Compared to LR parsers (Aho et al., 2007), RAGA has less number of states and less parser size. This is due to the fact that it performs shift-reduce operations with stack activities reduced to recursion handling. In addition, RAGA has no goto-transition on non terminals. Hence, their respective computational overhead and the construction of the goto-part of the parsing table are not included in the subset construction algorithm for RAGA.

RAGA is based on position parsing automata (PPA) as proposed in (Jabri, 2009) In addition, it handles recursion in a similar way as the one in recursion incorporated generalized parsers (RI) (Galves et al., 2006; Johnstone & Scott, 2007; Scott & Johnstone, 2005). However, compared to such approaches RAGA is distinguished by its annotation with translation schemes and the following properties:

(1) Compared to PPA, RAGA is considered as an extension since it handles left, embedded and direct right recursion, while PPA handles the embedded ones only. Furthermore, their handling approach is different. PPA handles recursion by state and transition instantiation while RAGA handles recursion by reduced stack activities. Finally, the reduced version of PPA (Jabri, 2012) has non deterministic behavior while RAGA has deterministic one. Such determinism is achieved by using look ahead symbols, upon the reduction actions of RAGA.

(2) Compared to RI, RAGA handles left and right recursion while RI handles embedded ones and follows different construction and parsing approach. In addition to stacks needed for recursion handling, in RI two parsing stacks are used while in RAGA no parsing stacks are used.

As a teaching tool, GCT has been experimented and compared against existing ones. It has been shown that GCT is distinguished by the following:

(1) GCT is based on concepts from finite and LR automata as well as syntax directed translation. Hence, it obeys strictly to theory and facilitates a smooth transition to practice.
Its use within the proposed teaching framework is consistent with the compiler construction phases and their respective order. In contrast, the existing tools are based on a particular approach, for examples:

- The suggested tool in (Mallozzi, 2005) is based on recursive descent approach.
- The suggested one in (Demaille & Levillain, 2008) is an extension of the well-known Bison tool (Corbett et al., 2003) and based on LALR grammar (Aho et al., 2007).
- A third tool suggested in (Morell & Middleton, 2003) follows recursive ascent approach that simulates tabular-less bottom up parsers.

In contrast to such tools and a similar one (Pinaki et al., 2011), GCT simulates a generic bottom-parser and maintains its inherent tables but with reduced size and overhead. Furthermore, compared to Lex and Yacc (Mason & Brown, 1990) GCCT is a pedagogical tool. Its input features regular and context-free grammars. Its construction approach is a direct mapping to an automaton. It produces as an output the transition graph and the parsing table respective to the constructed automaton, associated with textual information. Furthermore, it enables more experiments to be conducted by students within the framework of the compiler construction course. For example, students were asked to construct a parser using the same grammar (Example 9) and following the proposed approach as well as the SLR approach (Aho et al., 2007). It has been shown that the parser constructed according to our approach requires less construction time and less states (8) as compared to the one constructed by SLR (15 states). Furthermore, the ease of use of GCT as automated tool is demonstrated by the fact that it use reduced to an interaction context consisting of the textual representation of the context-free grammars without any modification. A graphical, tabular and textual information representing GCT are then displayed as an output.

6. Conclusion

In this paper, we have proposed and implemented a tool for teaching compilers. The tool is based on a new compiler construction approach that is characterized by its soundness, generality and efficiency. Having as an input, a generic grammar (Regular definitions or context-free grams), annotated by translation schemes, the proposed tool respectively reacts either as a scanner, a parser, or as a syntax directed translator. Such reaction proceeds as follows. First, it constructs a nondeterministic bottom–up automaton (AGA). The states and the transitions of AGA are defined based on concepts from the LR (0) items and the finite deterministic automata. Second, AGA is transformed into a reduced one (RAGA) in efficient way. Such automaton simulates the parsing behavior of the shift-reduce automata. Finally, the tool produces as an output the transition graph and the parsing / translation tables respective to RAGA. The experiments and the analysis of the proposed approach for have shown its superiority over similar ones, either in terms of its generality or in terms of its performance and ease of use. In addition, the tool has proved its practical application within a compiler teaching framework and in a way that tightly couples theory and practice. Since such experiments have emphasized the syntax analysis phase of compilers, further experiments, as a future work, are to be conducted to demonstrate the capability of the proposed tool in the subsequent compilation phases such as code generation.

References


